

BASILISK & PLASTIC MARINE DEBRIS TRACKING

Basilisk (Gerris) Users' Meeting 2025, University of Oxford

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PROF. TON VAN DEN BREMER (TU DELFT)

MISSION

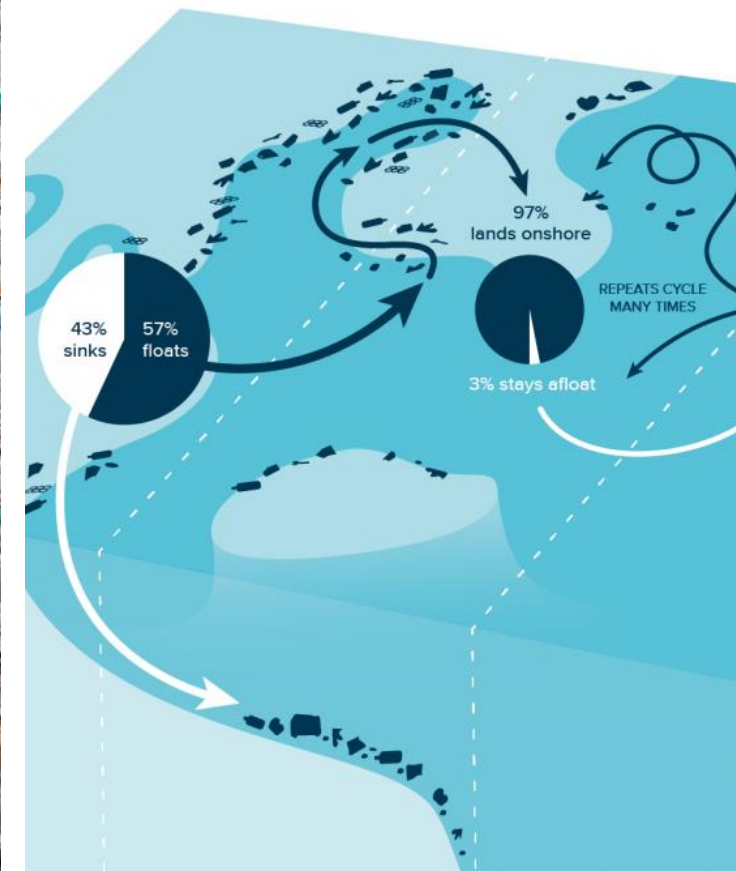
RID THE OCEANS OF PLASTIC

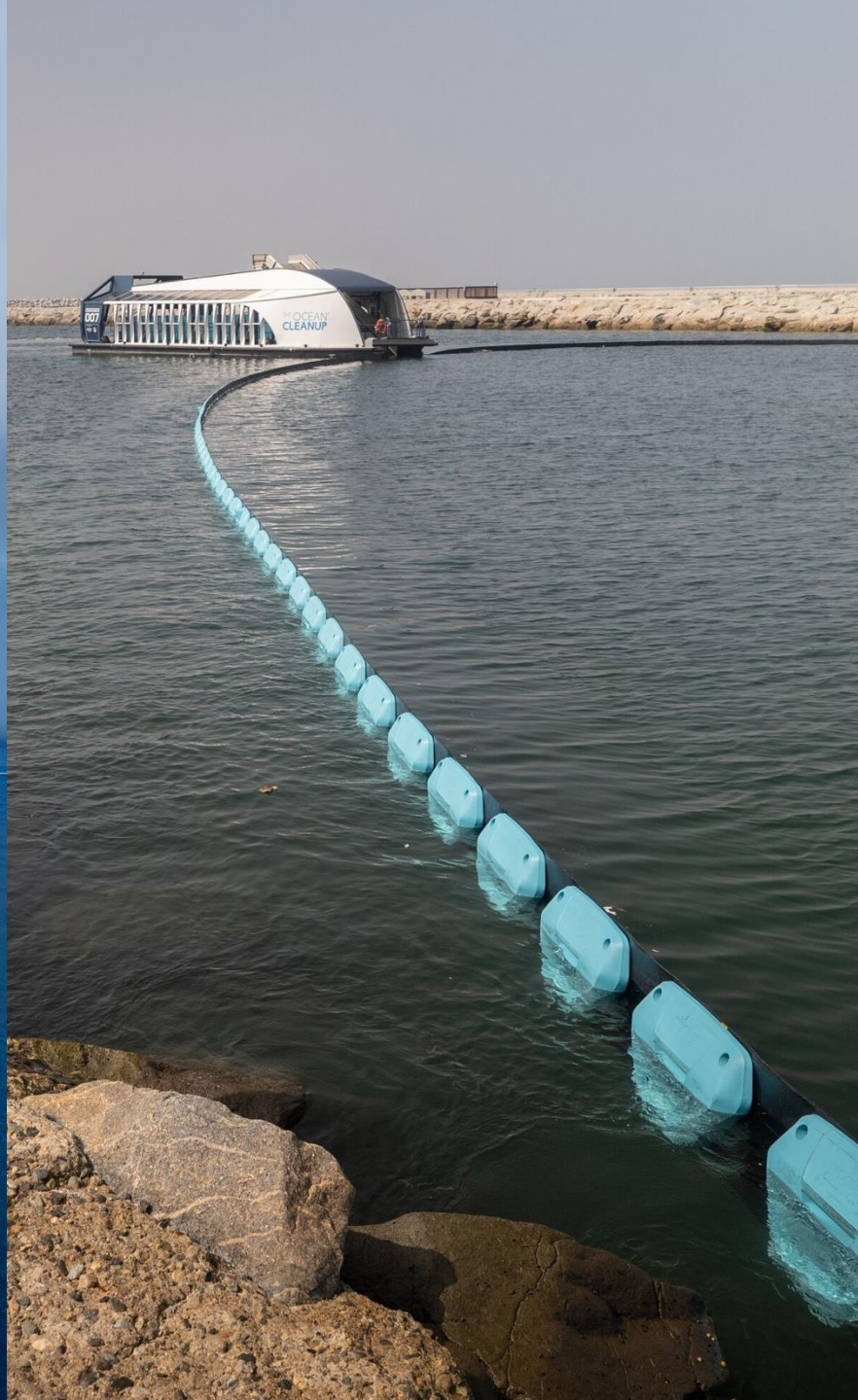




RIVERS

ARTERIES OF PLASTICS POLLUTION





DUAL STRATEGY FOR PLASTIC-FREE OCEANS

Cleanup systems for
ocean plastic gyres. In
rivers, **Interceptors**
capture plastics. We
are **targeting the**
world's most polluting
rivers.

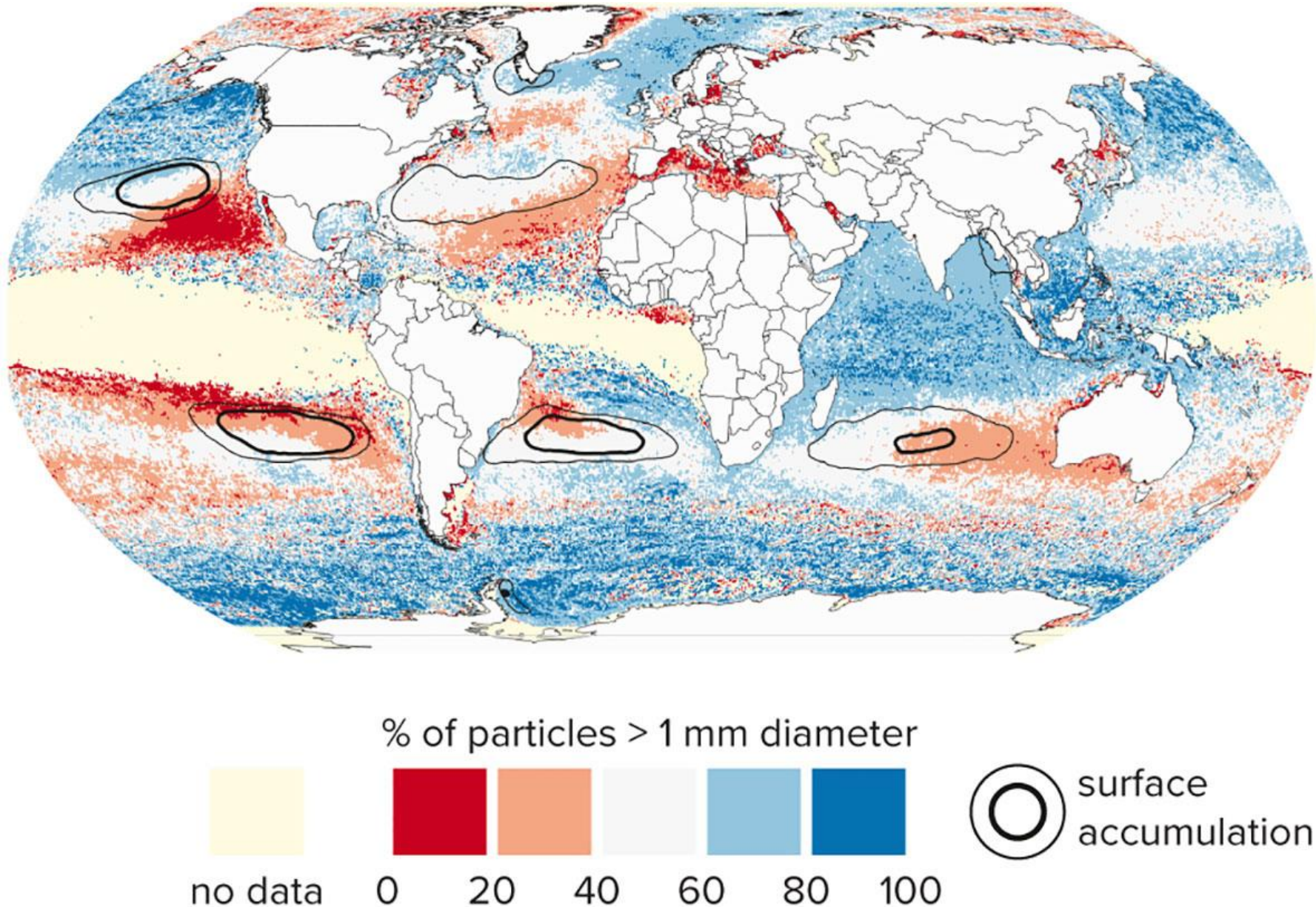


HOW TO MODEL THESE IN ALL SCALES OF THE OCEAN?



ADVECT¹

- OGCM + Lagrangian Particles
- Lagrangian advection of marine debris by currents
- Buoyancy & drag driven²
- Terminal rising velocity (fluid and the particles properties)



¹Klink, D., A. Peytavin, and L. Lebreton, 2022. Size Dependent Transport of Floating Plastics Modeled in the Global Ocean. *Front. Mar. Sci* 9.

²Dietrich, W.E., 1982. Settling velocity of natural particles. *Water resources research*, 18(6), pp.1615-1626.

PUTTING THINGS ON PERSPECTIVE

1/12 DEGREE



OCEAN OFFSHORE PROCESSES AND PLASTIC PARTICLES

1. Large-Scale Circulation

- **Subtropical Gyres:** Accumulation zones
- **Geostrophic Currents:** Persistent circular motion
- **Ekman Transport:** Wind-driven motion of surface waters.

3. Mesoscale and Submesoscale

- **Eddies (Mesoscale):** Large circular currents (~10–100 km) that trap or eject debris.
- **Frontal Zones:** Interfaces between water masses
- **Submesoscale Filaments:** Fast-moving features that can disperse debris over shorter timescales.

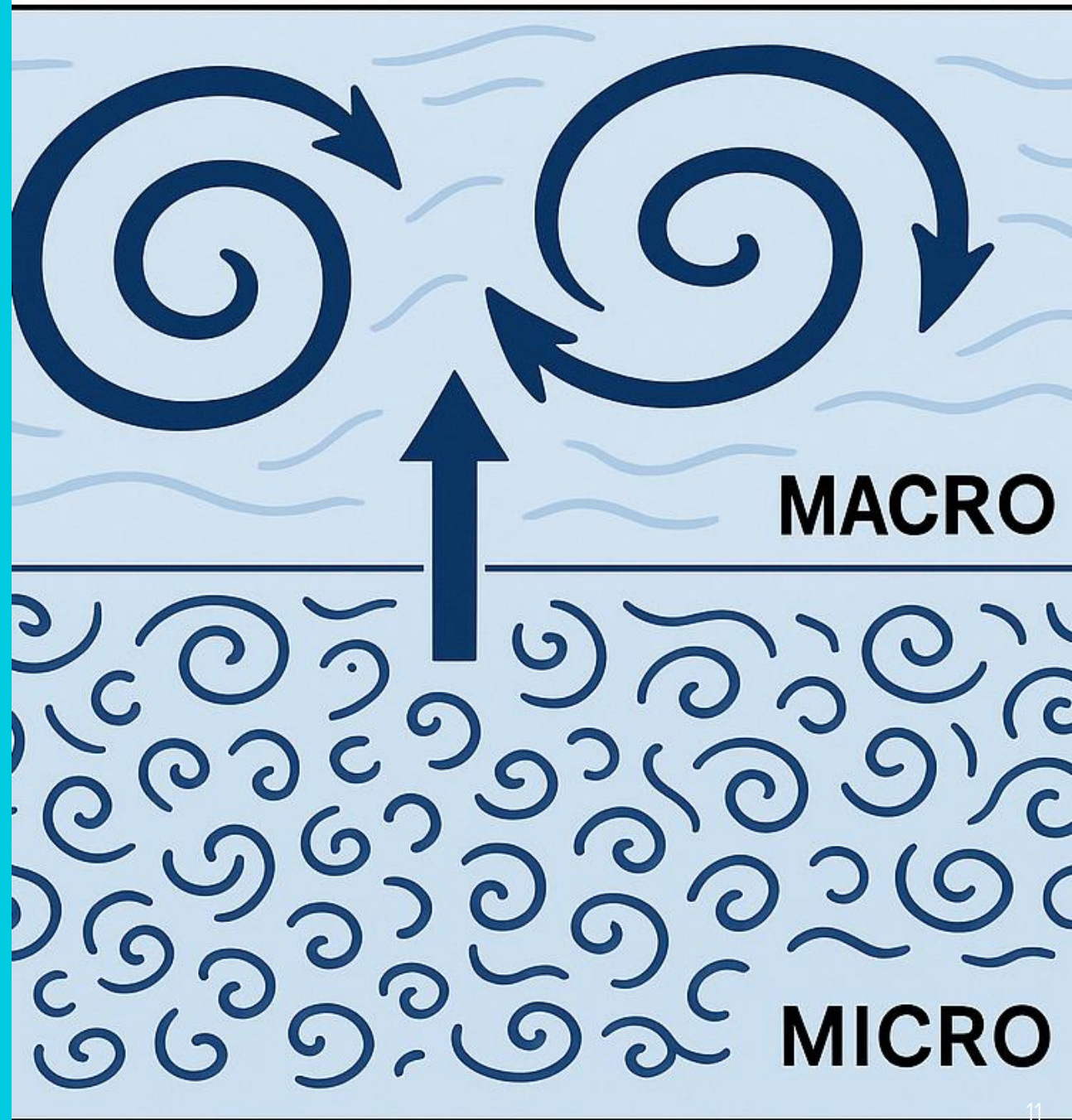
2. Wind and Wave-Induced

- **Stokes Drift:** Net motion of floating debris by wave
- **Windage:** Aerodynamic efforts on debris
- **Langmuir Circulation:** Wind-driven vortex pairs align floating debris into parallel windrows.

4. Vertical Transport & Mixing

- **Turbulent Mixing:** Surface turbulence (e.g., from storms) pushes debris down temporarily.
- **Eddy-Driven Subduction:** Downwelling zones of eddies
- **Diurnal Thermocline Variability:** Day-night heating cycles.

INFORMATION TRANSFER



FLUID

$$\rho_f \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = -\nabla p + \nabla \cdot (2\mu_f \mathbf{D}) + \sigma \kappa \delta_s \mathbf{n} + \mathbf{g} + \cancel{\mathbf{f}_{p \rightarrow f}}$$

$$\frac{\partial \rho_f}{\partial t} + \nabla \cdot (\rho_f \mathbf{u}) = 0$$

$$\nabla \cdot \mathbf{u} = 0$$

SOLID

$$M \frac{d\mathbf{V}}{dt} = (M - m_f) \mathbf{g} + m_f \frac{D\mathbf{u}}{Dt} + 3\pi d_p \mu (\mathbf{u} - \mathbf{V})$$

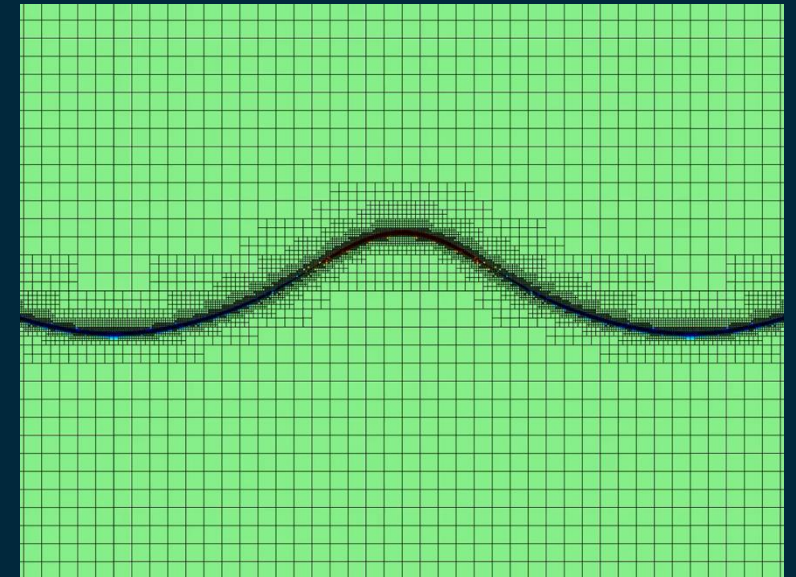
$$+ \frac{1}{2} \rho_f m_f \frac{d(\mathbf{u} - \mathbf{V})}{dt} + \frac{3}{2} d_p^2 (\pi \mu \rho)^{\frac{1}{2}} \left(\int_0^t \frac{\frac{d(\mathbf{u} - \mathbf{V})}{d\zeta}}{(t - \zeta)^{\frac{1}{2}}} d\zeta \right)$$

³S. Popinet. An accurate adaptive solver for surface-tension-driven interfacial flows. *Journal of Computational Physics*, 228, 16, 2009.

⁴M. R. Maxey and J. J. Riley. Equation of motion for a small rigid sphere in a nonuniform flow. *Physics of Fluids*, 26, 883-889, 1983.

EULER-LAGRANGE (EL)

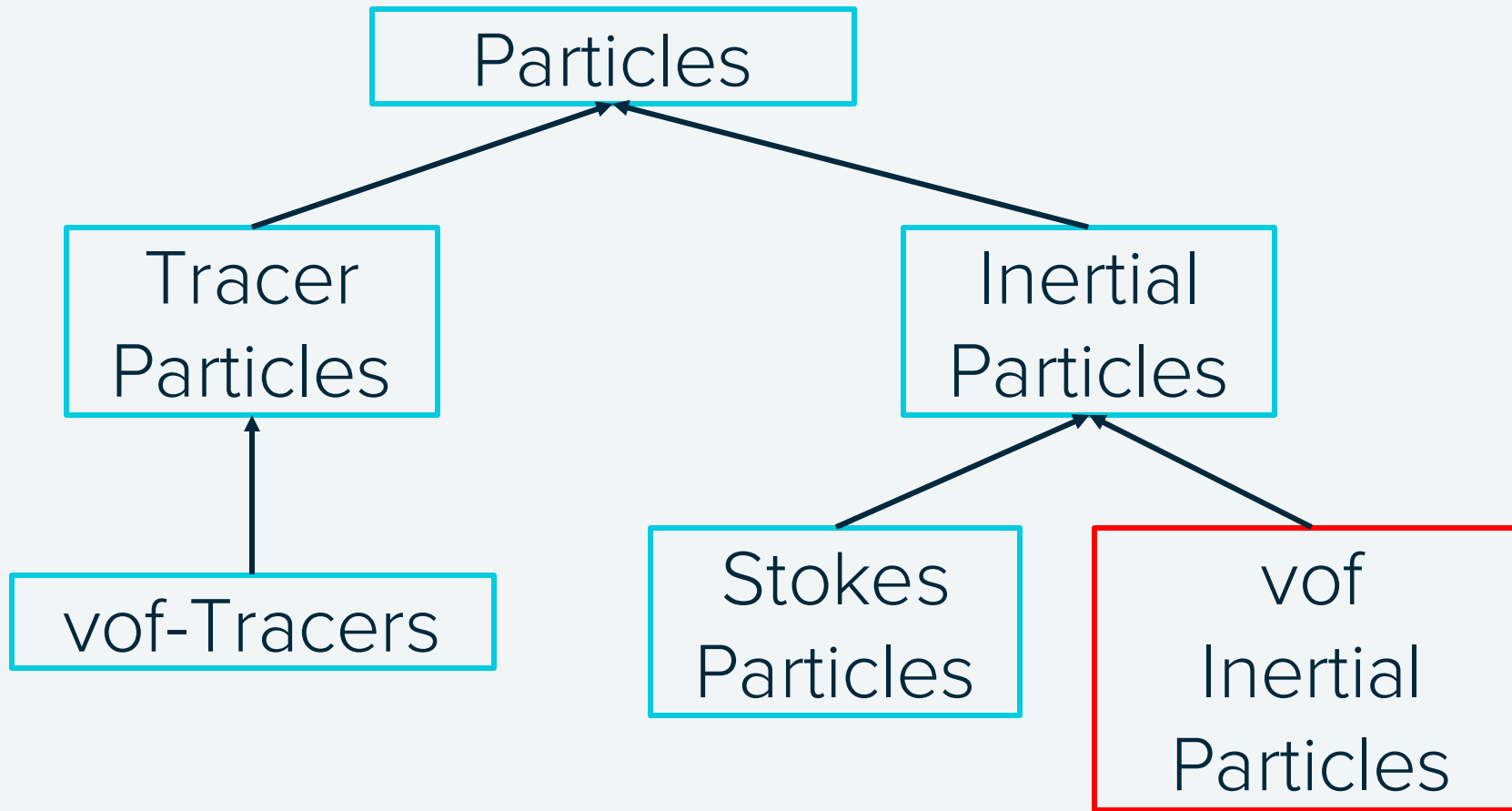
- DNS of canonical waves with Basilisk³
- Navier-Stokes + interfacial flow solver + Geometrical VoF + Quad/Octrees data structure
- Maxey-Riley⁴ Point-Particle



<http://basilisk.fr/sandbox/popinet/wave.c>

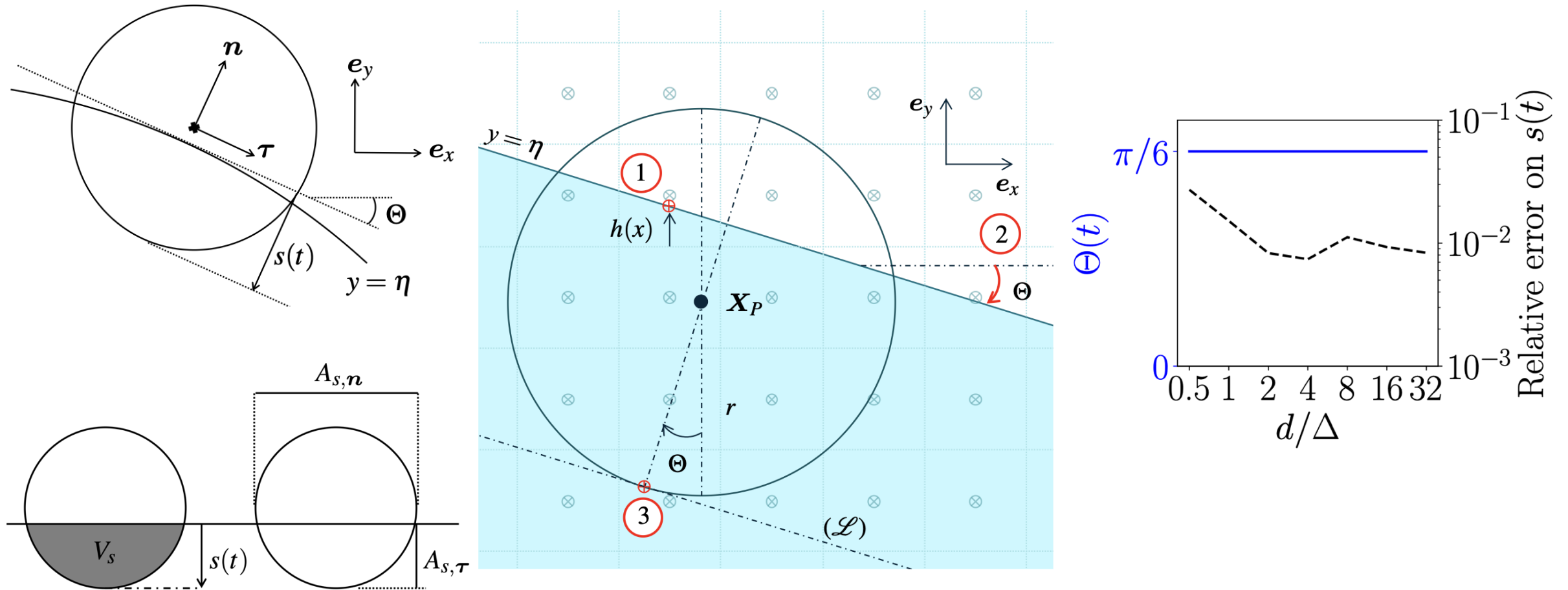
INHERITENCE FROM ANTOON'S SANDBOX

<http://basilisk.fr/sandbox/Antoonvh/README>



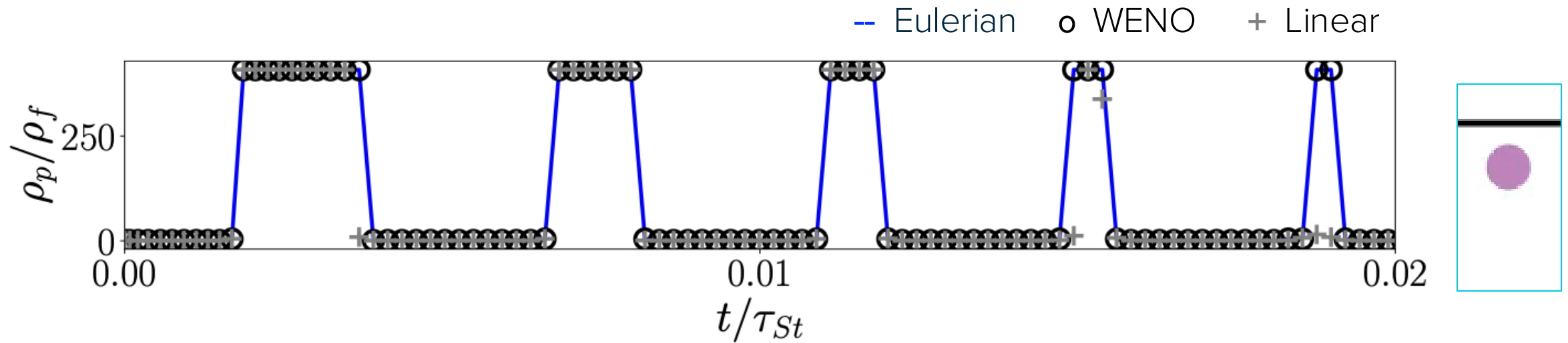
- Dilute regime (one-way coupled)
- Non Stokesian
- Macro plastics ($> 2\text{cm}$)
- Negligible effects of surface tension
- $d \ll \lambda$

HEIGHT-FUNCTION⁵ FOR HYDRODYNAMIC FORCES



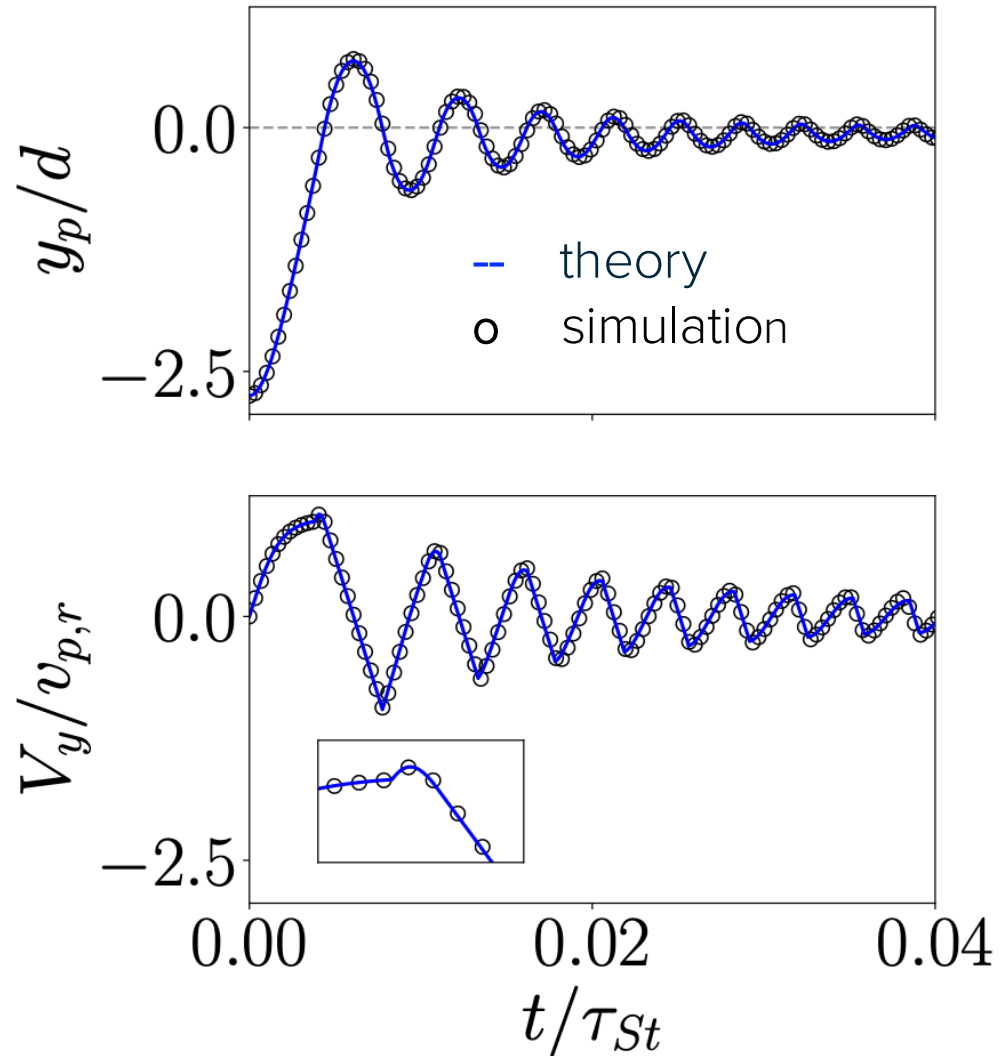
⁵Popinet, S. (2009). An accurate adaptive solver for surface-tension-driven interfacial flows. *Journal of Computational Physics*, 228.

5TH ORDER WENO⁷ INTERPOLATION

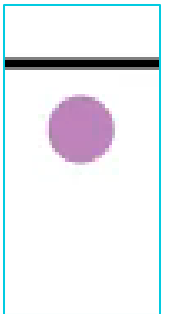
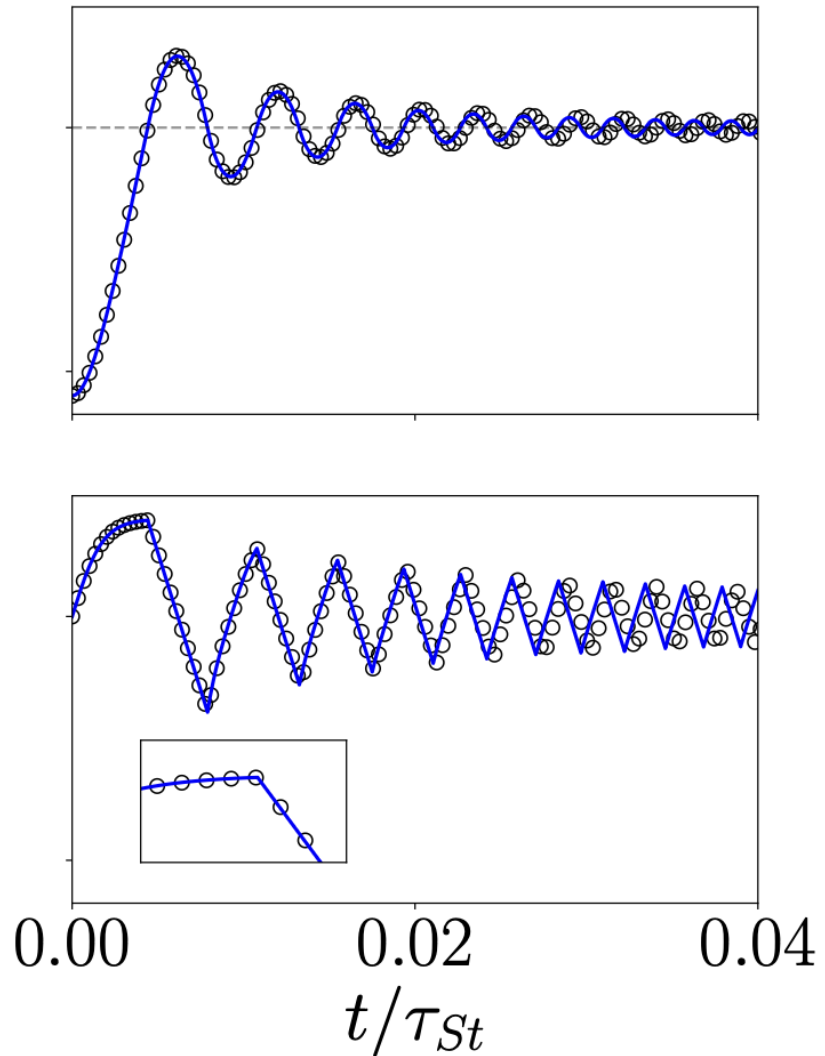


⁷Shu, C.-W. and Osher, S. (1988). Efficient implementation of essentially non-oscillatory shock-capturing schemes. *Journal of Computational Physics*, 77, 439–471.

5TH ORDER WENO⁷

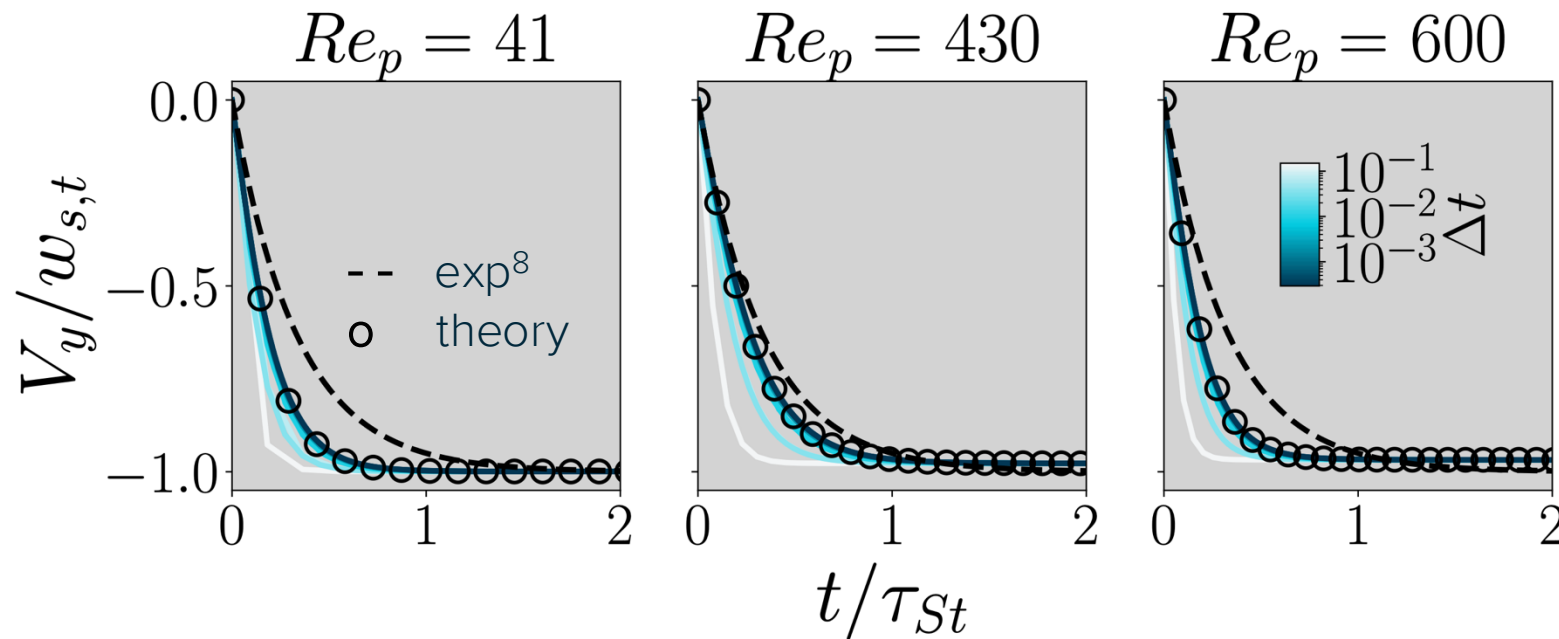


LINEAR



⁷Shu, C.-W. and Osher, S. (1988). Efficient implementation of essentially non-oscillatory shock-capturing schemes. *Journal of Computational Physics*, 77, 439–471.

SETTLING VELOCITY TEST



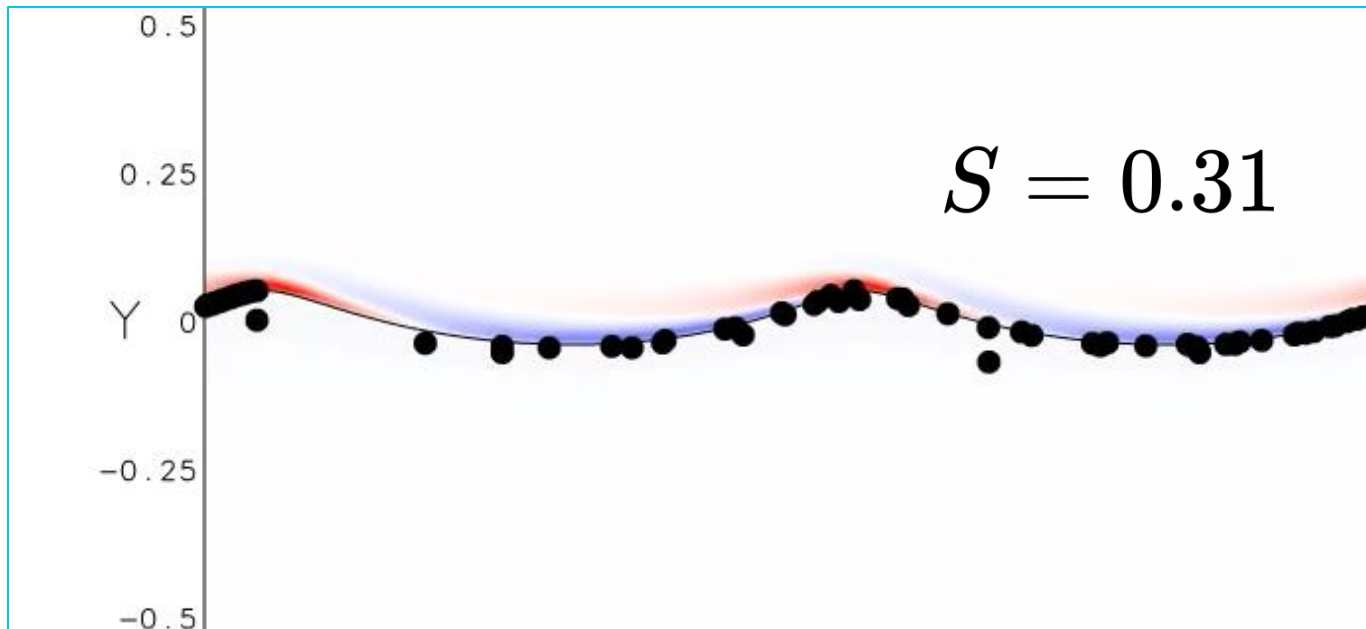
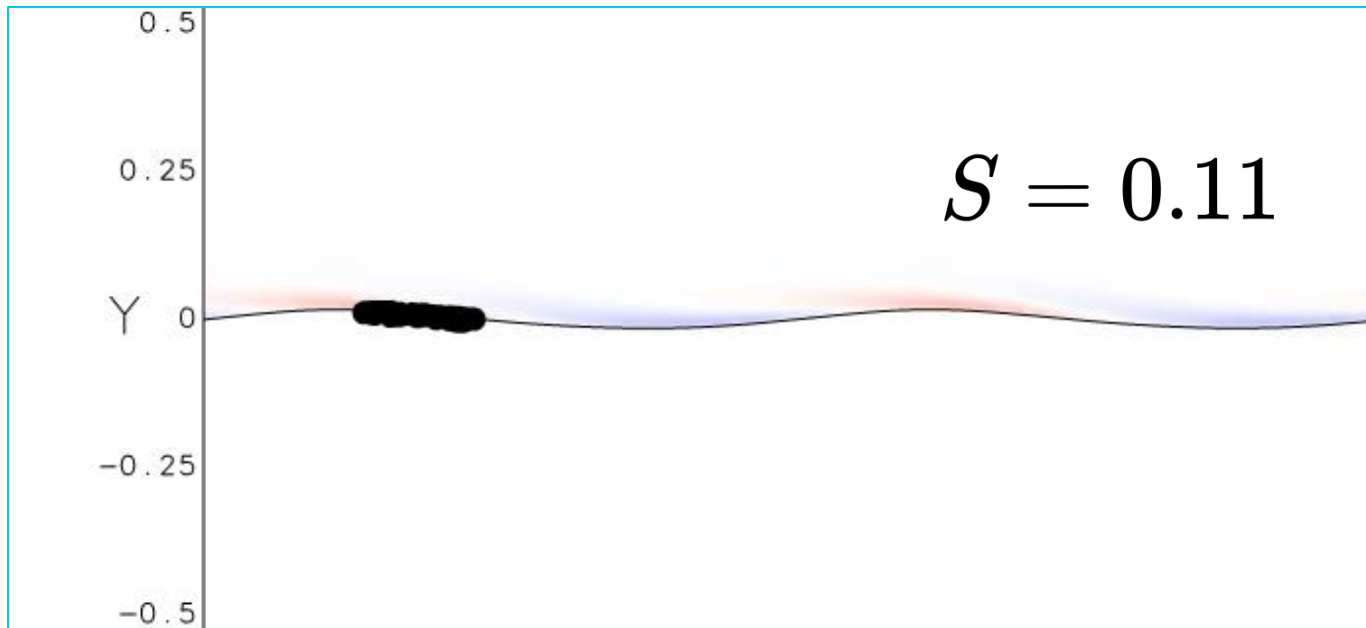
⁸Mordant, N., & Pinton, J.-F. (2000). Velocity measurement of a settling sphere. *The European Physical Journal B-Condensed Matter and Complex Systems*, 18, 343–352.

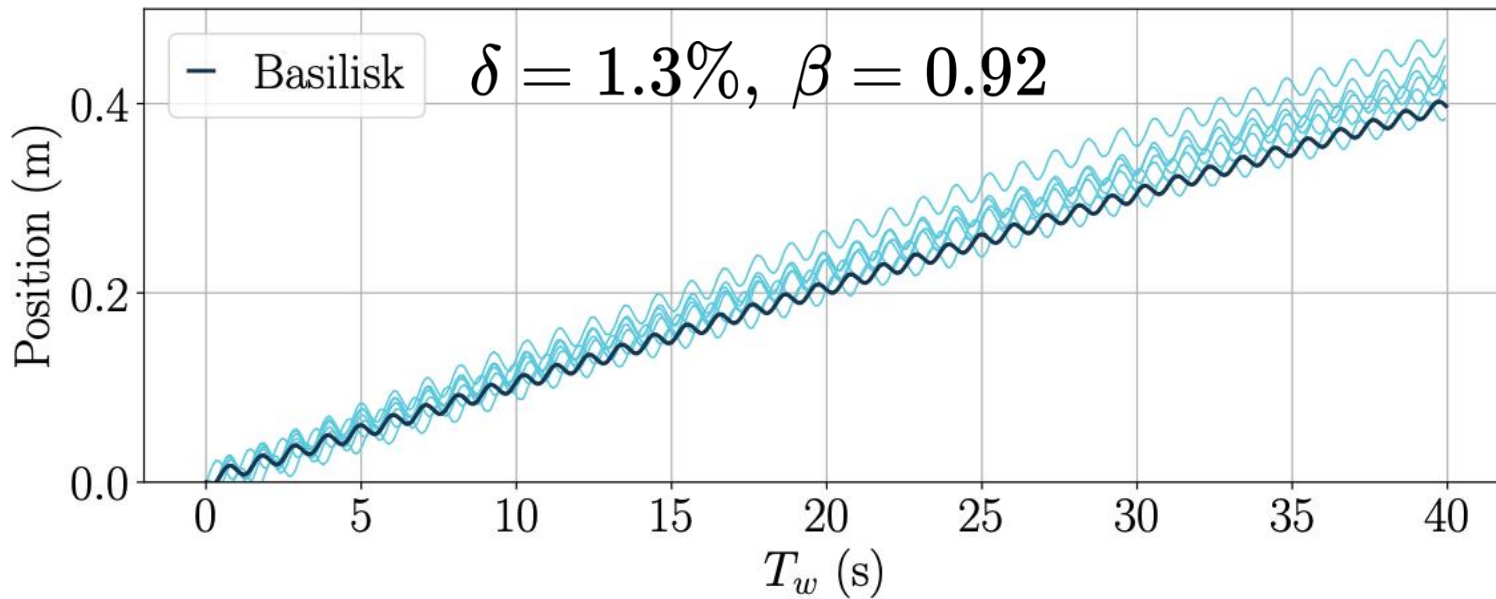
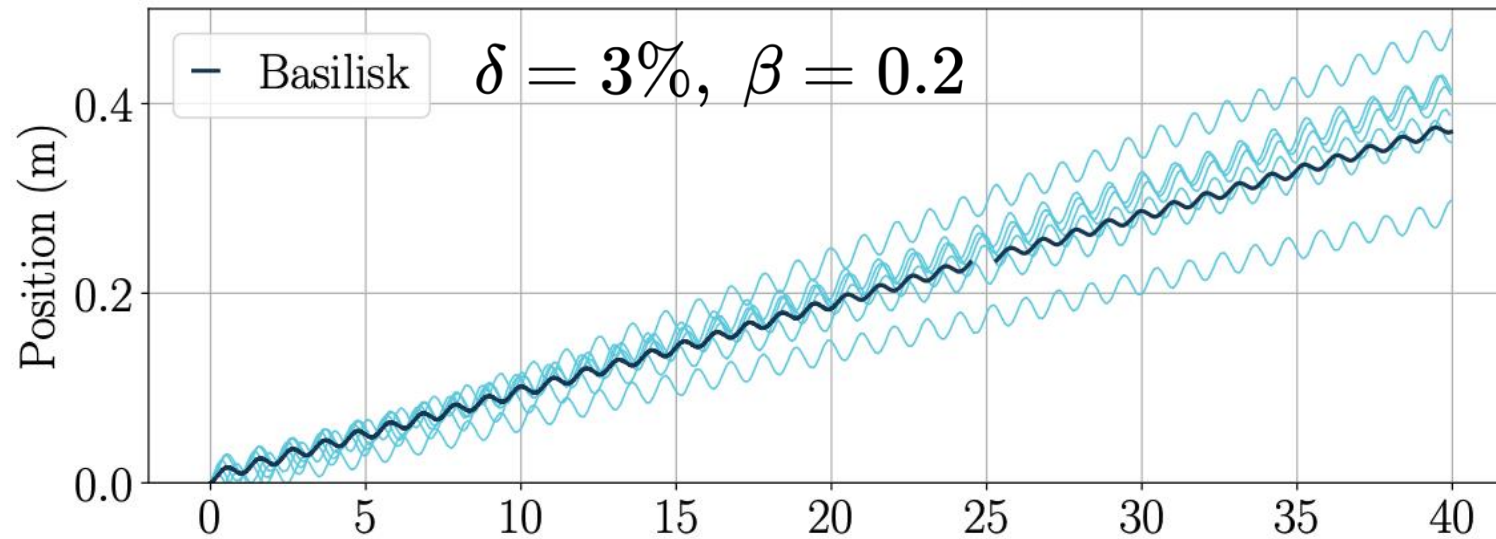
WAVE-INDUCED
MOTION OF
RELATIVELY
SMALL PLASTICS

$$\delta = \frac{d}{\lambda} \leq 3\%$$

$$\beta = \frac{\rho_p}{\rho_w}$$

$$0.2 \leq \beta \leq 0.9$$

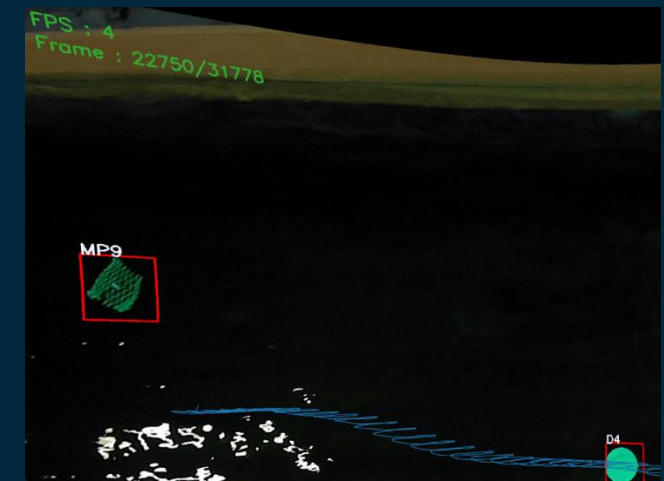




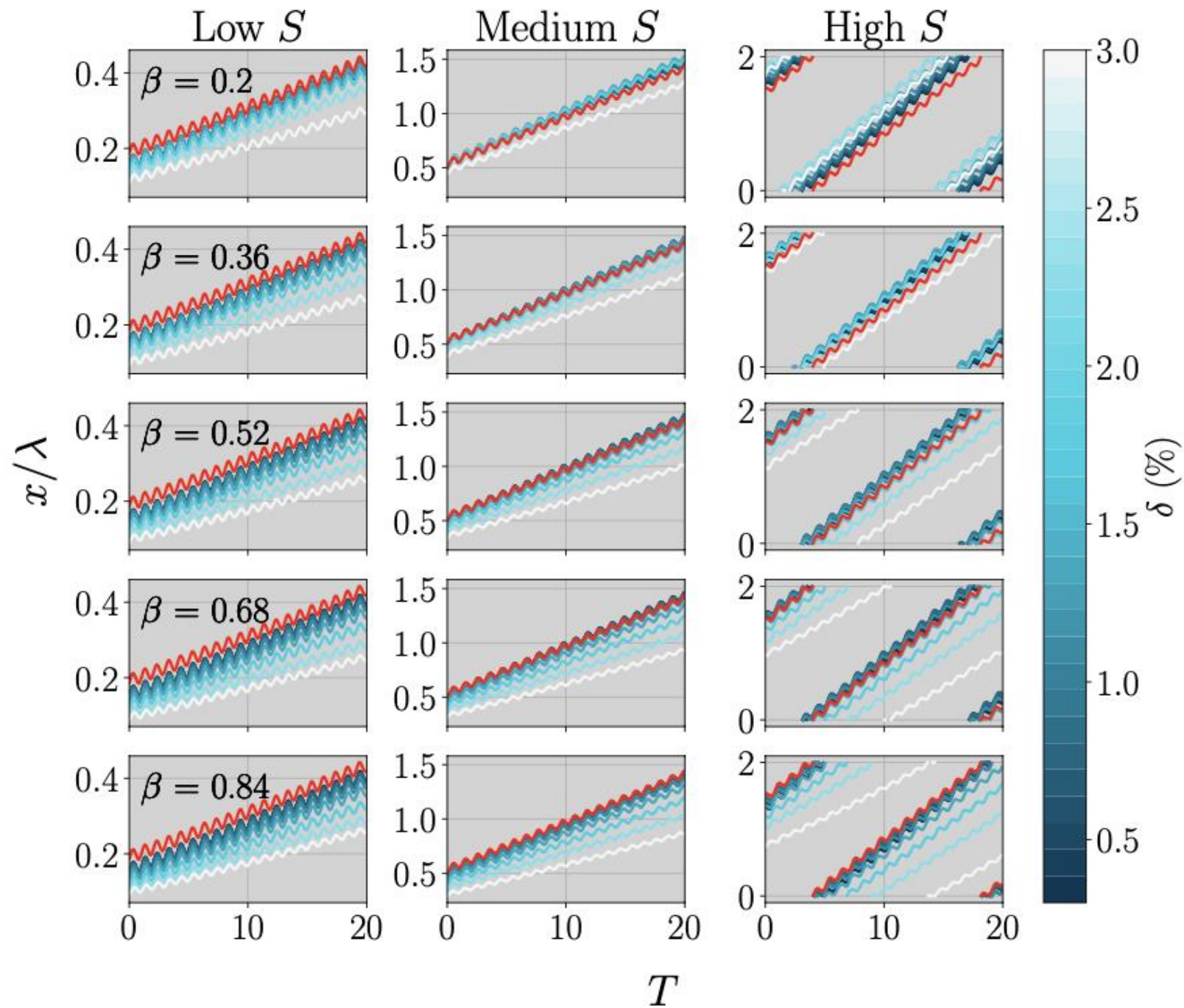
INERTIAL PARTICLES

EXPERIMENTS⁹ (BLUE)
VS
SIMULATION (BLACK)

$$S = 0.16$$

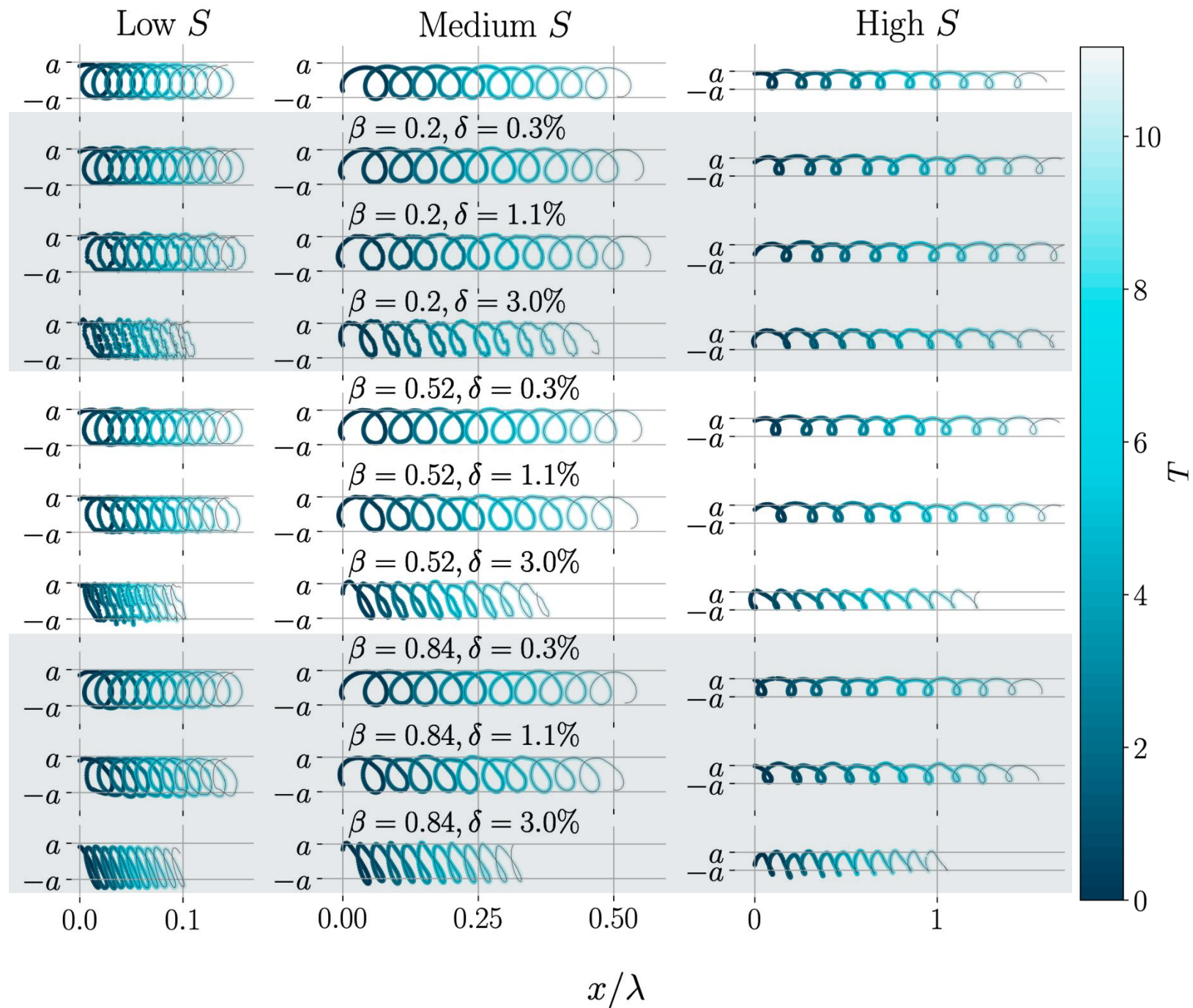
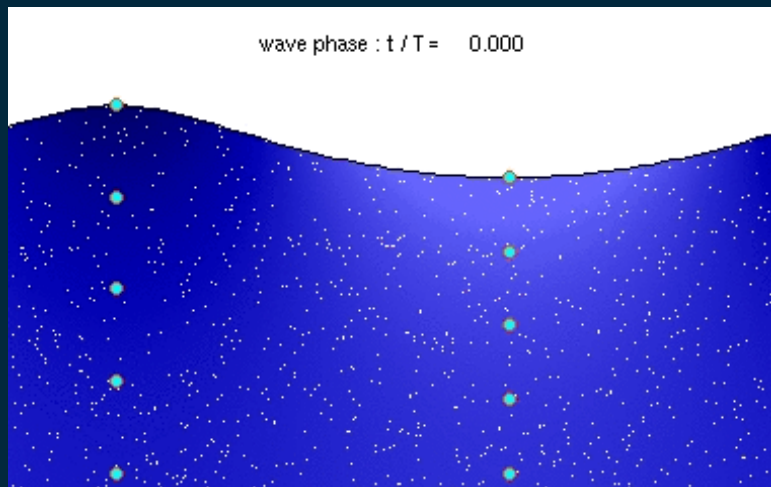


⁹Calvert, R. *et al.* (2024). A laboratory study of the effects of size, density, and shape on the wave-induced transport of floating marine litter. *Journal of Geophysical Research: Oceans* 129.

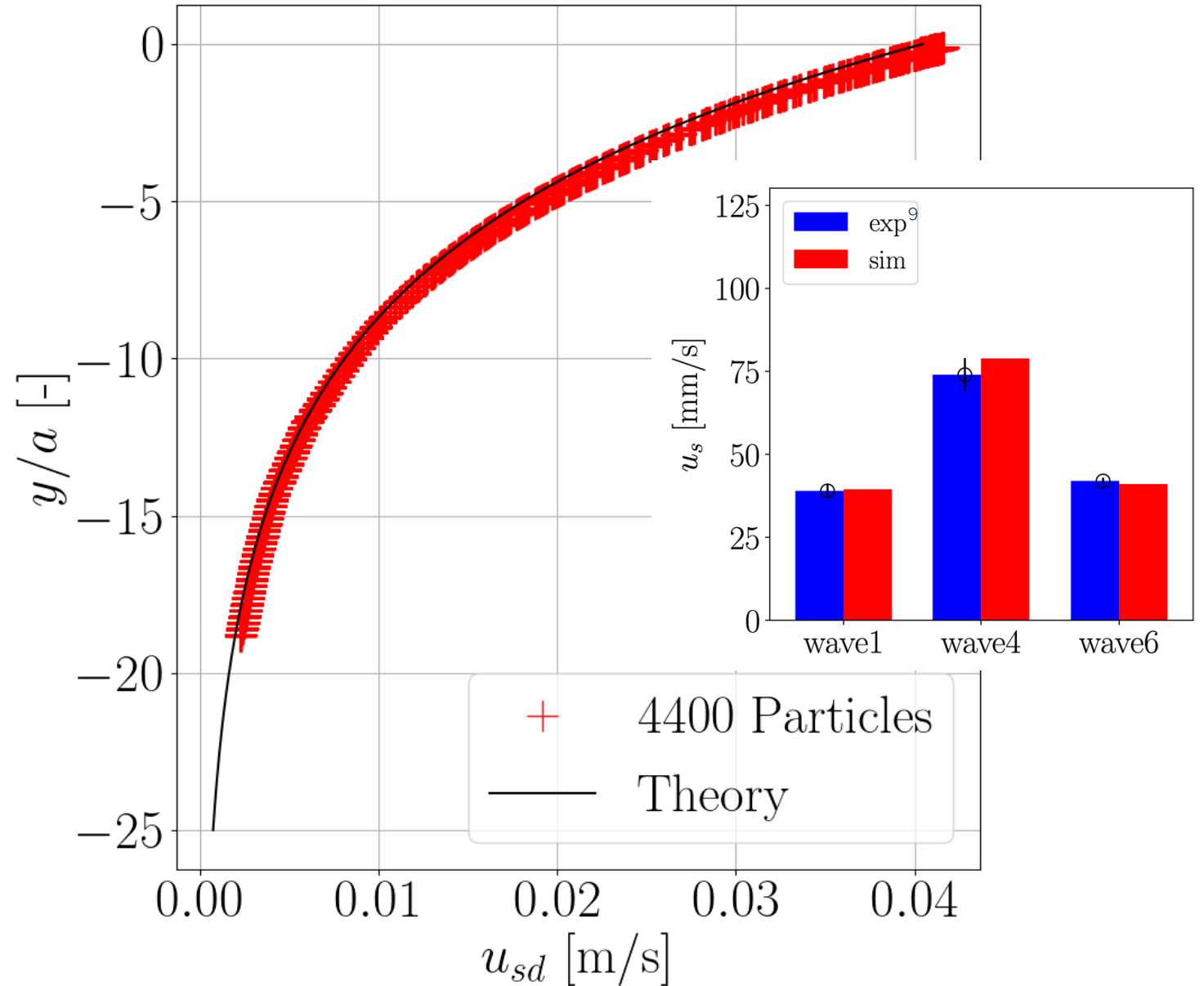
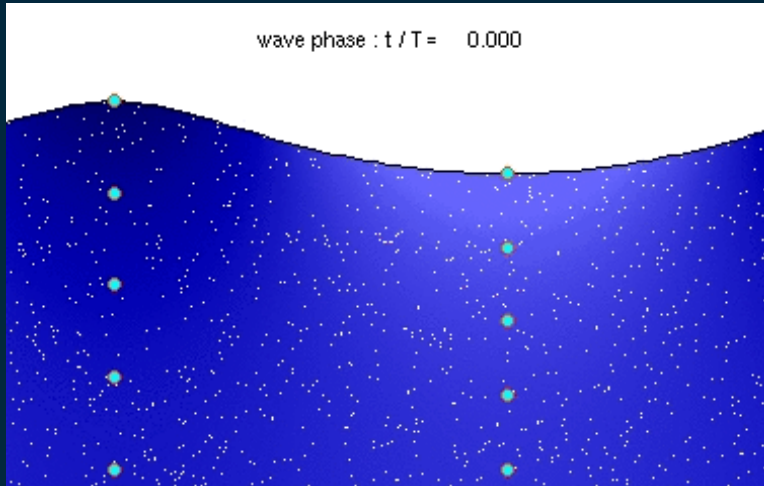


PASSIVE TRACERS
VS
INERTIAL PARTICLES

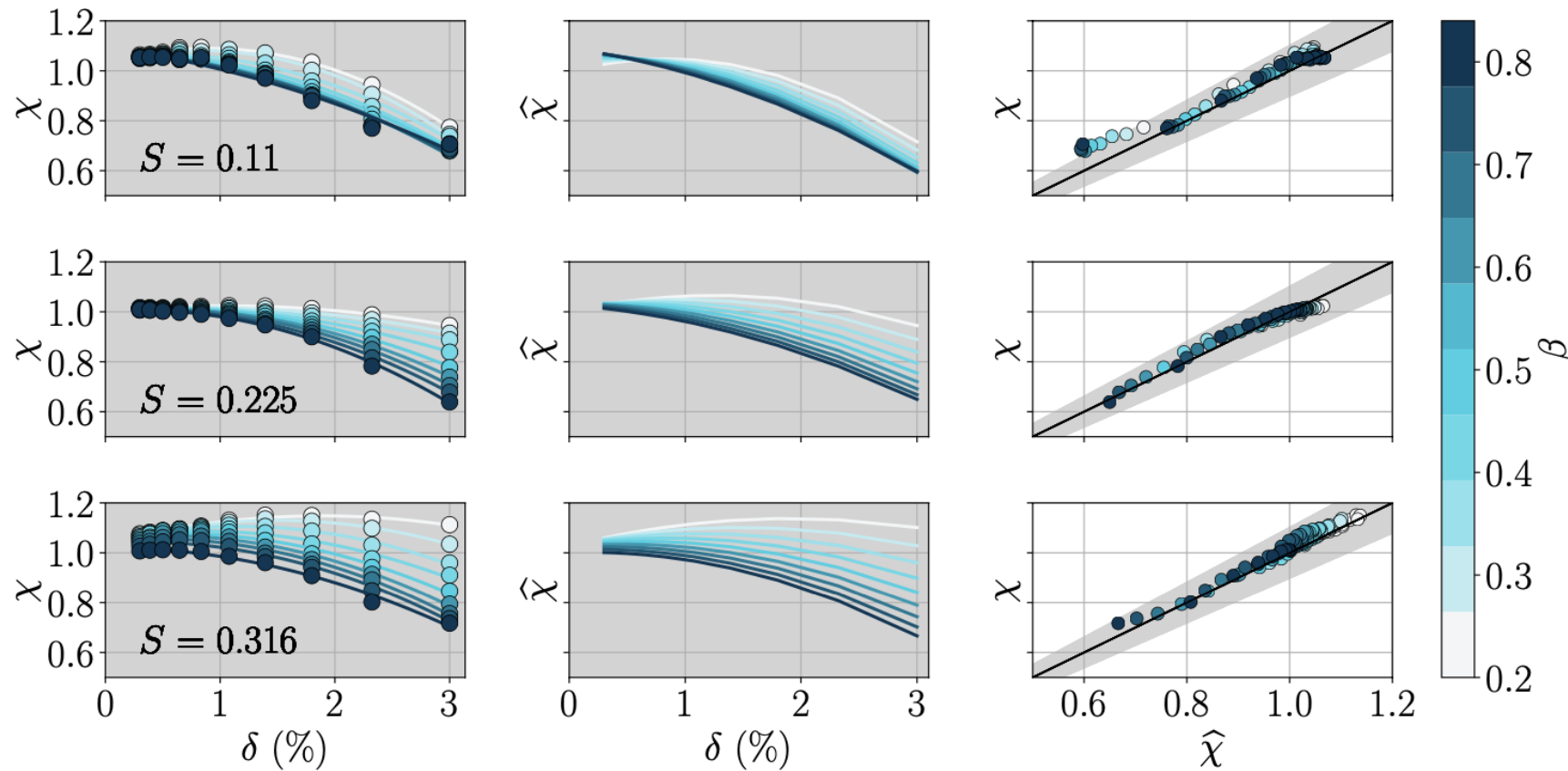
WAVE-INDUCED MOTION



STOKES DRIFT (PASSIVE TRACERS)



DRIFT AMPLIFICATION FACTOR

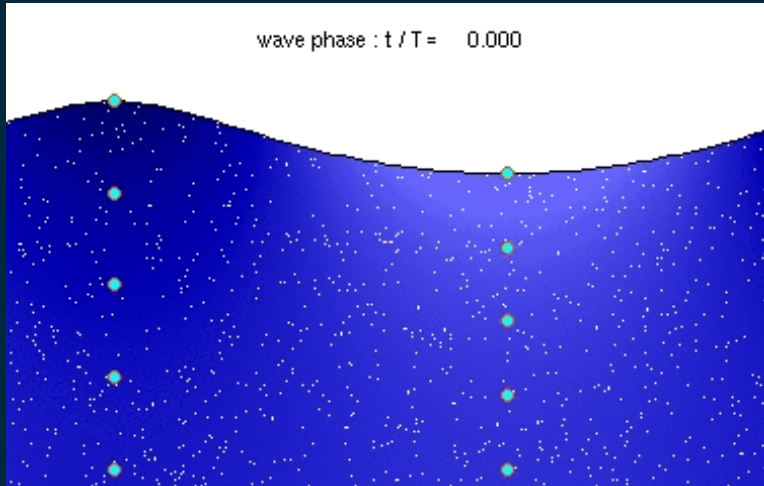


$$\chi = \frac{\widetilde{V_{p,x}}}{u_s(y=0)}$$

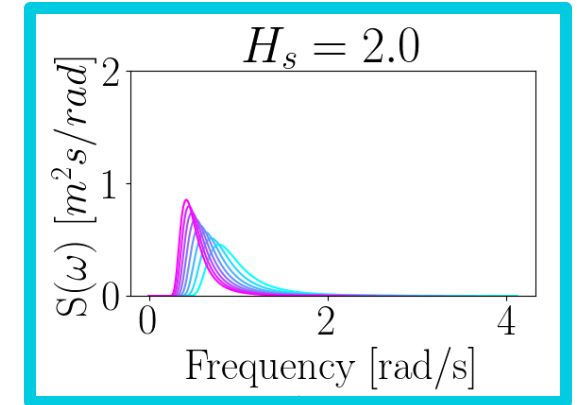
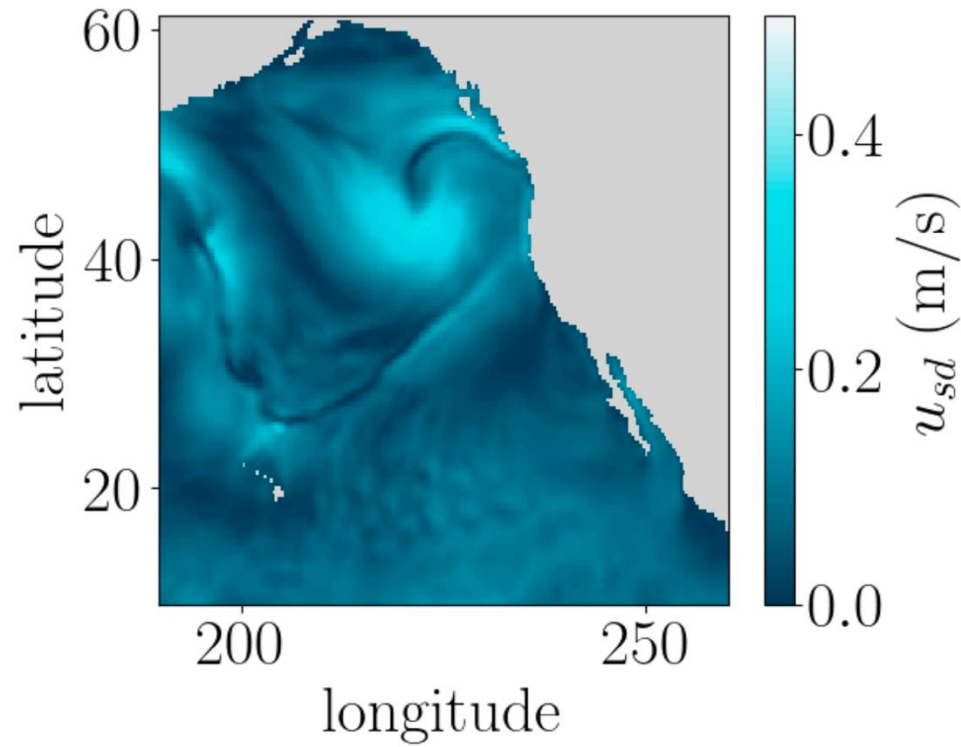
$$\chi = f(\delta; S, \beta)$$

$$\hat{\chi}(\delta; S, \beta) = \hat{a}(S, \beta)\delta^2 + \hat{b}(S, \beta)\delta + \hat{c}(S, \beta)$$

STOKES DRIFT & WAVEWATCH III



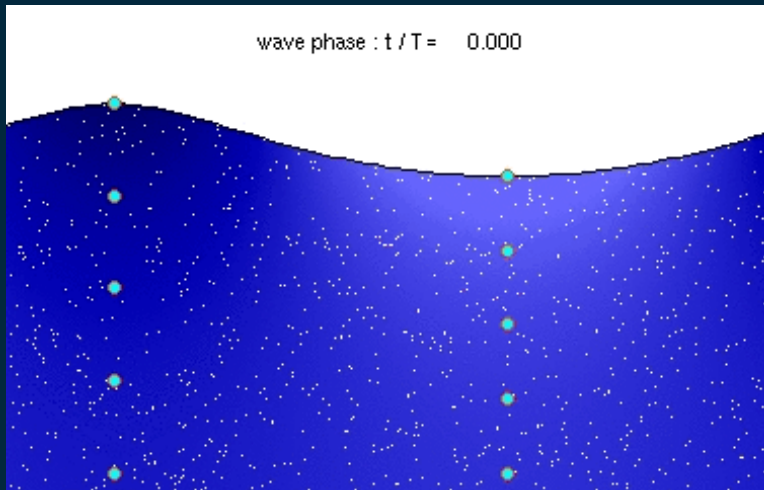
- Spectral integration over all resolved wavenumbers and directions,
- Finite-depth correction for finite depth effects.



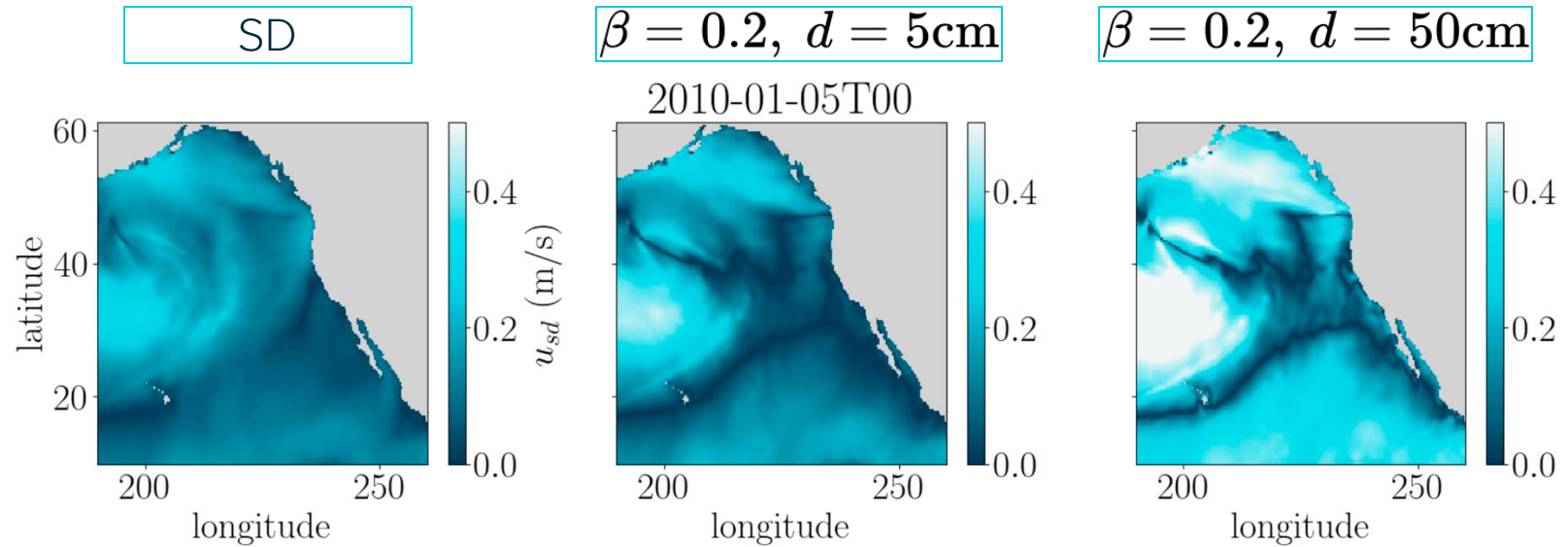
$$U_{ssx} = g \iint \sigma \frac{\cosh(2kd_w)}{\sinh^2(kd_w)} k \cos(\theta) F(k, \theta) dk d\theta$$

$$U_{ssy} = g \iint \sigma \frac{\cosh(2kd_w)}{\sinh^2(kd_w)} k \sin(\theta) F(k, \theta) dk d\theta$$

MODIFIED STOKES DRIFT & WAVEWATCH III

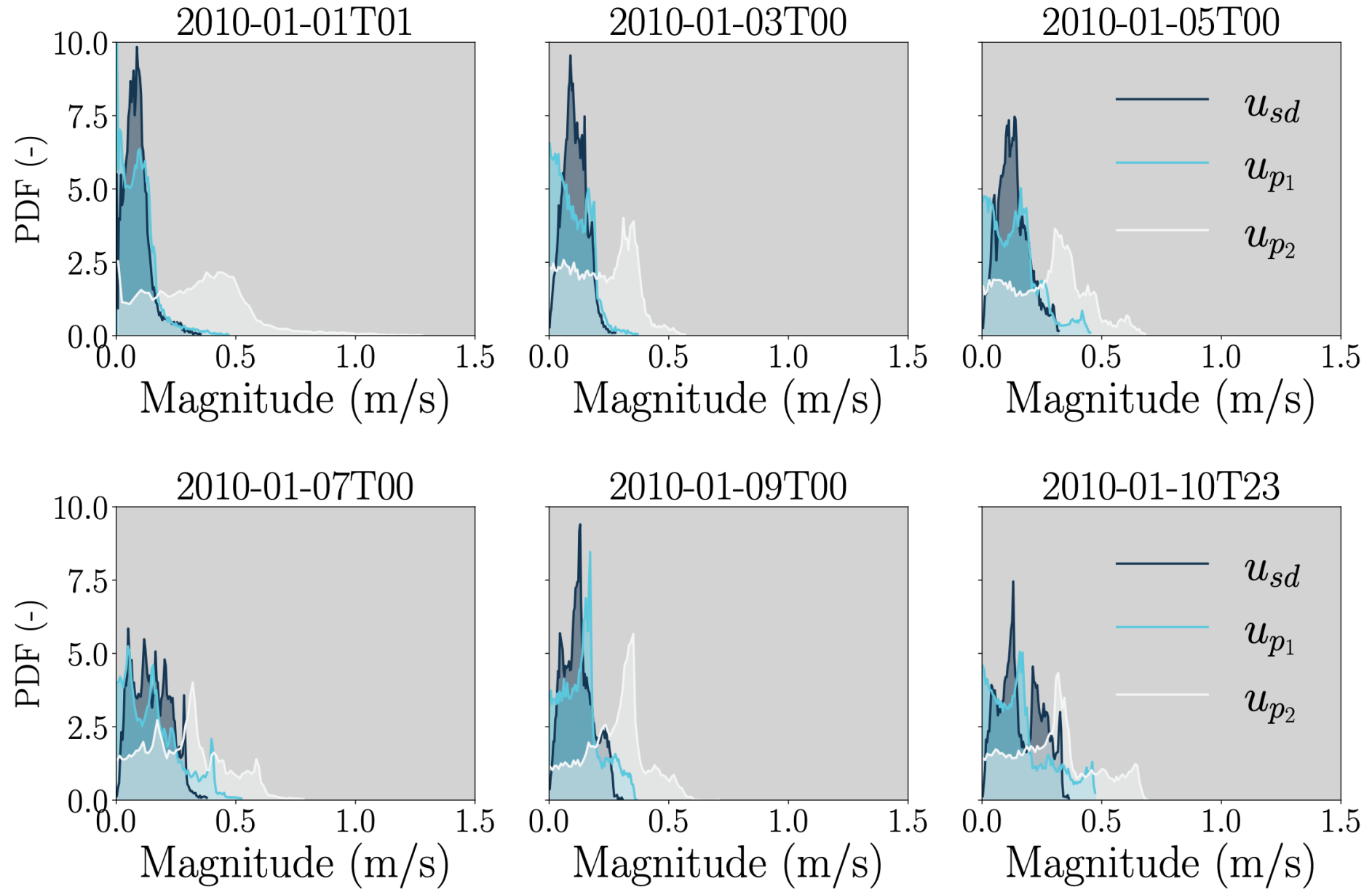


- Spectral integration over all resolved wavenumbers and directions,
- Finite-depth correction for finite depth effects.



$$U_{ssx} = g \iint \sigma \frac{\cosh(2kd_w)}{\sinh^2(kd_w)} k \cos(\theta) \hat{\chi}(k, \theta) F(k, \theta) dk d\theta$$

$$U_{ssy} = g \iint \sigma \frac{\cosh(2kd_w)}{\sinh^2(kd_w)} k \sin(\theta) \hat{\chi}(k, \theta) F(k, \theta) dk d\theta$$



CONCLUSION

- We combined DNS with experimental data to study wave-induced drift of plastics
- By computing the ratio $\hat{\chi}(\delta; S, \beta)$ we quantify inertia influence on the modified Stokes drift field.
- This enables evaluation of plastic transport and accumulation driven by wave dynamics.
- Our approach reveals how spectral and directional wave properties affect the convergence of inertial plastics.

A Volume of Fluid / Point-Particle approach for the simulation of the wave-induced drift of plastic marine debris

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(Dated: 7 July 2025)

THE OCEAN[®] CLEANUP