

Wetting effects on the dynamics of droplets and bubbles at surfaces

Yifan Han¹, Kerstin Eckert^{1,2}, Gerd Mutschke¹

1 Helmholtz-Zentrum Dresden-Rossendorf, Institute of Fluid Dynamics, Dresden, Germany

2 Technical University of Dresden, Institute of Process Engineering and Environmental Technology, Dresden, Germany

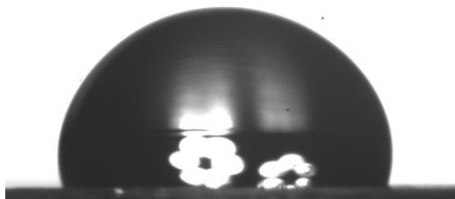


1. Wetting

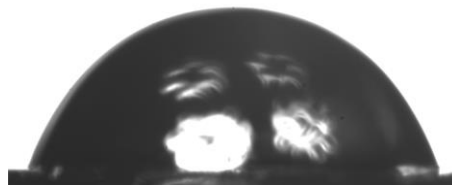
Wetting describes how a liquid spreads on or adheres to a solid surface.



Static contact angle (θ_s)



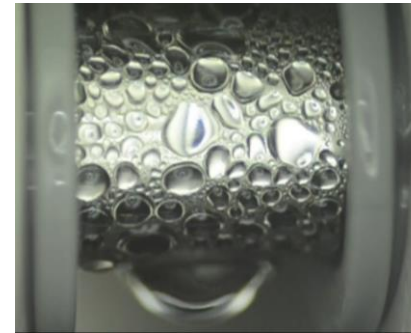
Hydrophobic
 $\theta_s > 90^\circ$



Hydrophilic
 $\theta_s < 90^\circ$

Applications:

➤ Droplets

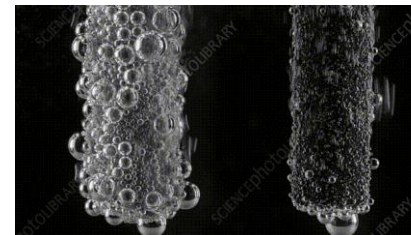


Cooling



Coating

➤ Bubbles

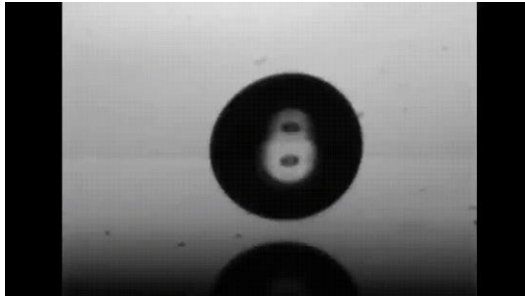


Water Electrolysis

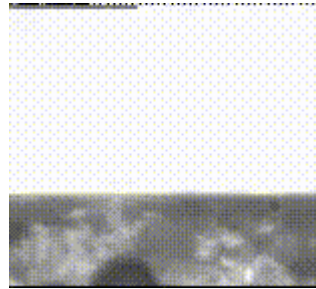


Boiling

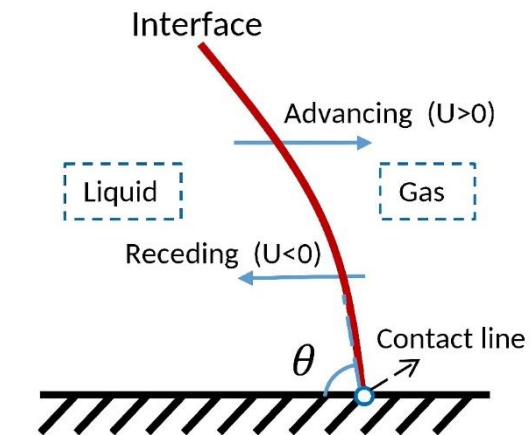
2. Dynamic wetting



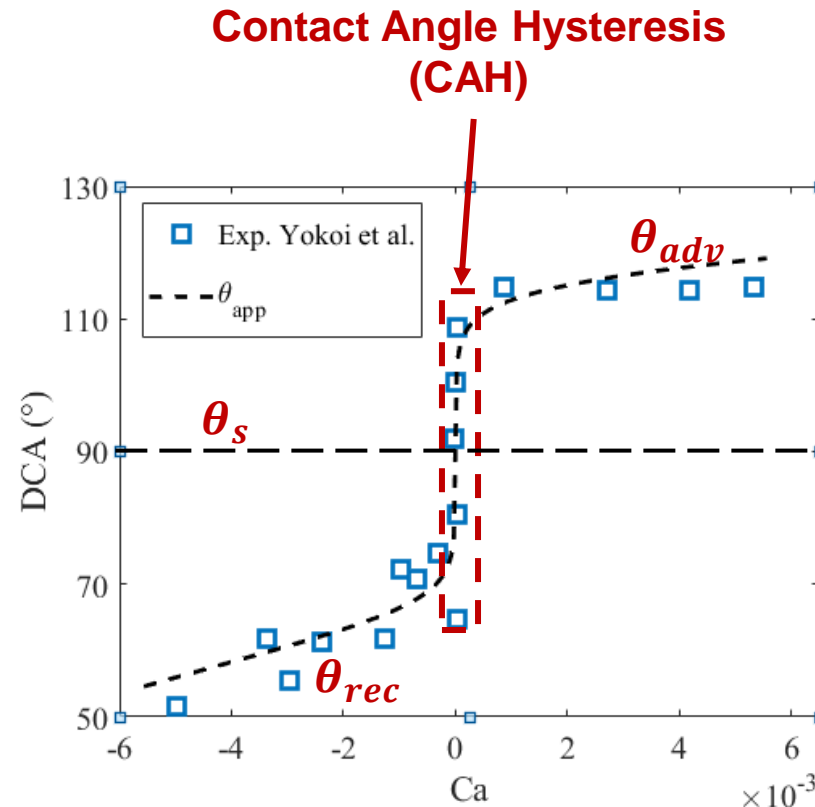
Droplet impact



Bubble growth



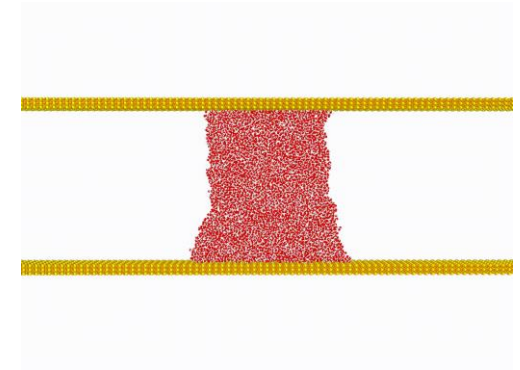
Sketch of contact line



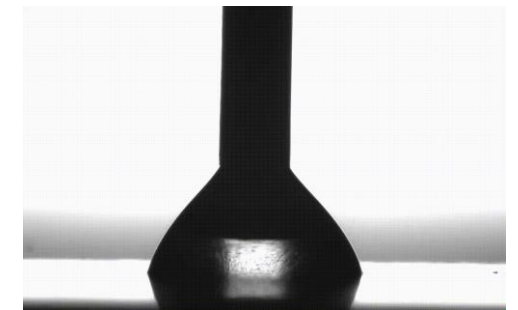
Contact angle VS Capillary number (contact velocity)

$$Ca = \mu U_{CL} / \gamma$$

Microscopic



Macroscopic



[1] Yokoi et al. Physics of Fluids, 2009, 21(7).

[2] Li et al. Colloids and Surfaces A: Physicochemical and Engineering Aspects 673 (2023): 131879.

3. Literature Review

➤ Level-Set Method:

Interface normal projection

Spelt. 2005 JCP, Yokoi et al. 2009 POF, Zhang et al. 2020 JCP.

➤ Phase-Field Method

Surface-energy formulation

Ding et al. 2007 PRE, Yue et al. 2010 JFM, Yue et al. 2011 POF.

➤ Volume of Fluid Method

Height function

Afkhami et al. 2009 JCP,

Dupont & Legendre 2010 JCP,

Fullana et al. 2025.

(Interfacial cell center velocity)

(Interpolation velocity at $f=0.5$)

(Time derivative of the contact line)

**Continuous
interface**

**Sharp
interface**

4. Droplet spreading on a surface

Axisymmetric setup



Volume of Fluid method

$$\rho = (1 - f)\rho_g + f\rho_l, \quad \mu = (1 - f)\mu_g + f\mu_l.$$

Piecewise linear interface construction (PLIC) method.

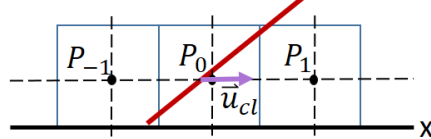
Flow fields & interface motion

$$\nabla \cdot \vec{u} = 0,$$

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} = -\frac{1}{\rho} \nabla p + \frac{1}{\rho} \nabla \cdot \{ \mu [\nabla \vec{u} + (\nabla \vec{u})^T] \} + \vec{g} + \gamma \kappa \vec{n} \delta_{\Sigma},$$

Contact line velocity

x-axis



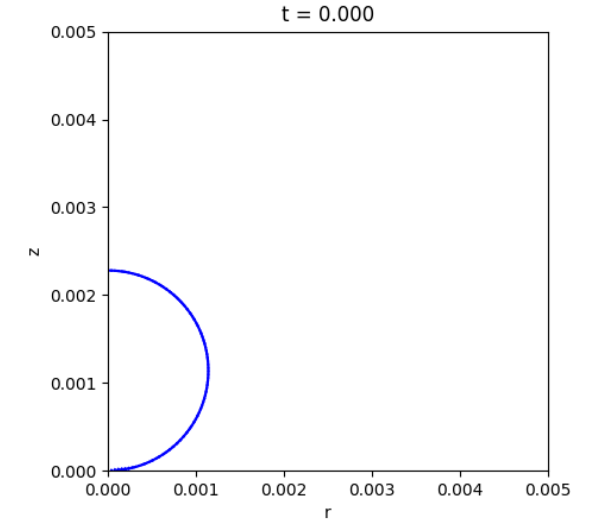
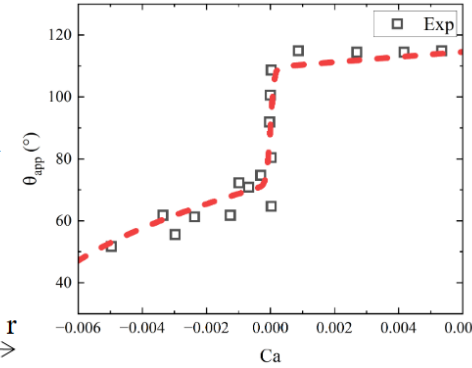
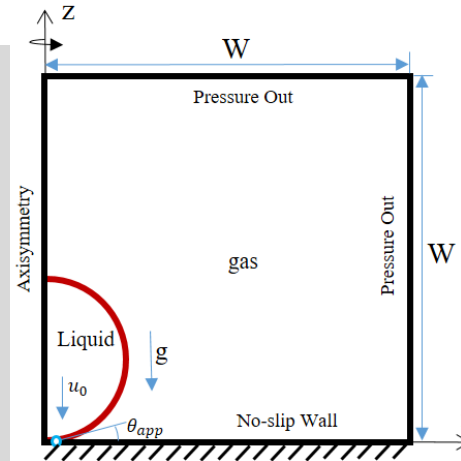
Linear Interpolation

Apparent contact angle

$$\theta_{local} = \arccos \left\{ \cos \theta_s - \frac{\xi Ca}{\mu} - \frac{C_{pin} \tanh(C * Ca)}{\gamma} \right\}$$

$$\theta_{app}^3 = \theta_{local}^3 + 9Ca \ln(\epsilon)$$

[2] Dwivedi et al. Physical Review Fluids, 2022, 7(3): 034002.

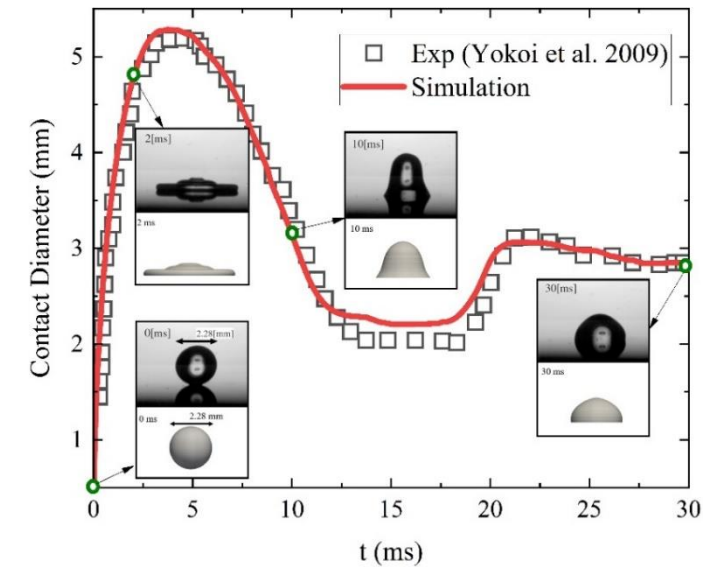


Weber number $We=31.7$

Initial radius: $R = 1.14 \text{ mm}$

Initial velocity: $V = 1.0 \text{ m/s}$

$\theta_s(^{\circ})$	$\theta_a(^{\circ})$	$\theta_r(^{\circ})$	$\xi_a(\text{Pa} \cdot \text{s})$	$\xi_r(\text{Pa} \cdot \text{s})$	C	ϵ
90	109.5	72	0.002	0.002	2×10^4	1.0×10^7

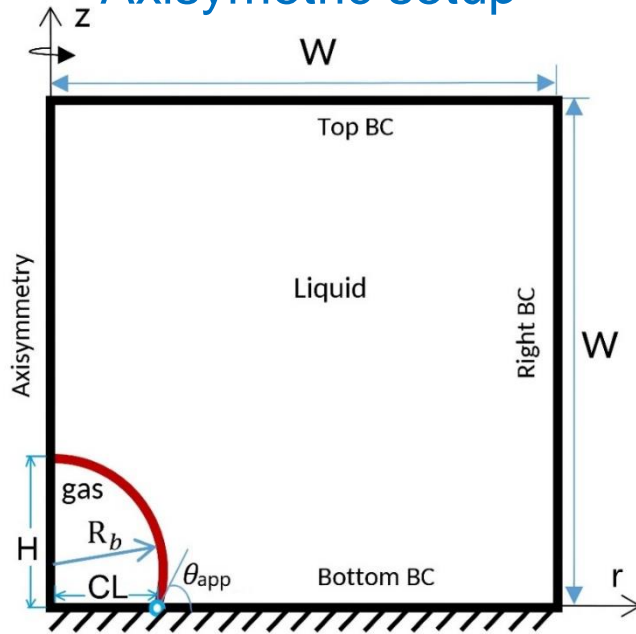


[1] Yokoi et al. Physics of Fluids, 2009, 21(7).

5. Bubble growth in oversaturated liquids



Axisymmetric setup



[1] Gennari et al. Chemical Engineering Science 259 (2022): 117791.

Flow fields & interface motion

$$\nabla \cdot \vec{u} = \dot{m} \left(\frac{1}{\rho_g} - \frac{1}{\rho_l} \right) \delta_{\Sigma},$$

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} = -\frac{1}{\rho} \nabla p + \frac{1}{\rho} \nabla \cdot \{ \mu [\nabla \vec{u} + (\nabla \vec{u})^T] \} + \frac{\vec{f}_\gamma}{\rho} + \vec{g},$$

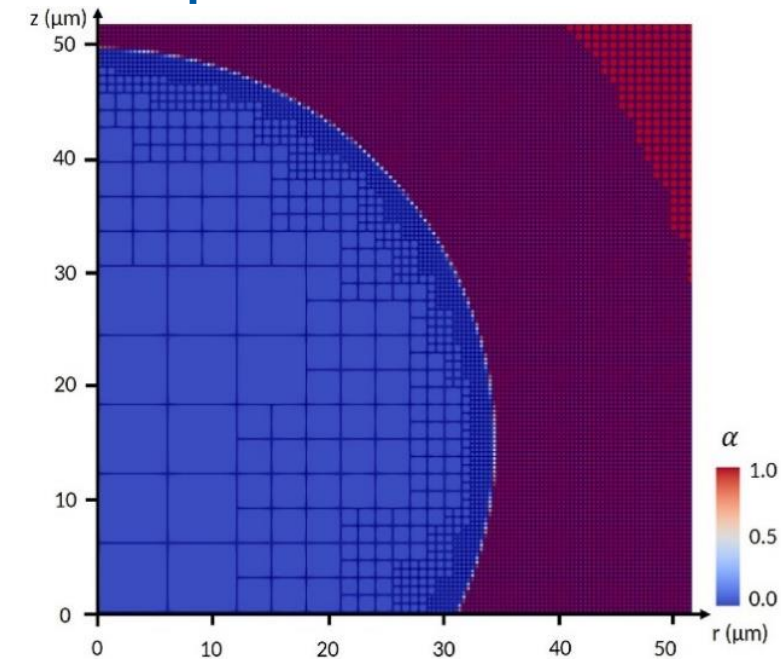
Species transport & mass flux

$$\frac{\partial \alpha}{\partial t} + \nabla \cdot (\alpha \vec{u}) = -\frac{\dot{m}}{\rho_l} \delta_{\Sigma},$$

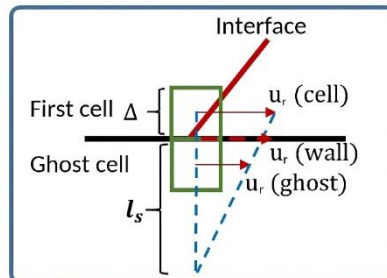
$$\frac{\partial c}{\partial t} + \vec{u} \cdot \nabla c = \nabla \cdot (D \nabla c) - \frac{\dot{m}}{M_a} \delta_{\Sigma},$$

$$\dot{m} = \frac{M_g D}{1 - \rho_g / \rho} \frac{\partial c}{\partial \vec{n}_{\Sigma}},$$

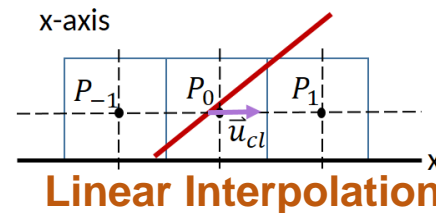
Adaptive Mesh Refinement



Navier-slip BC



Contact line velocity



Apparent contact angle

$$\theta_{local} = \arccos \left\{ \cos \theta_s - \frac{\xi Ca}{\mu} - \frac{C_{pin} \tanh(C * Ca)}{\gamma} \right\} \quad \text{Microscopic}$$

$$\theta_{app}^3 = \theta_{local}^3 + 9Ca \ln(\epsilon) \quad \text{Macroscopic}$$

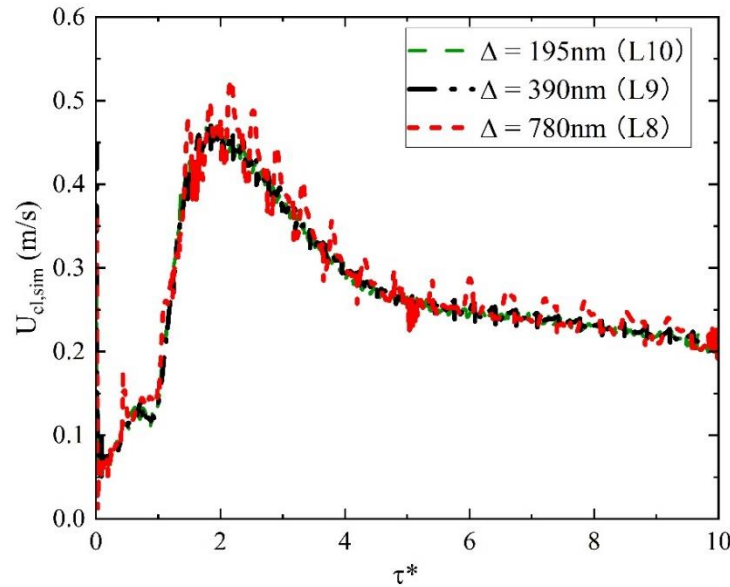
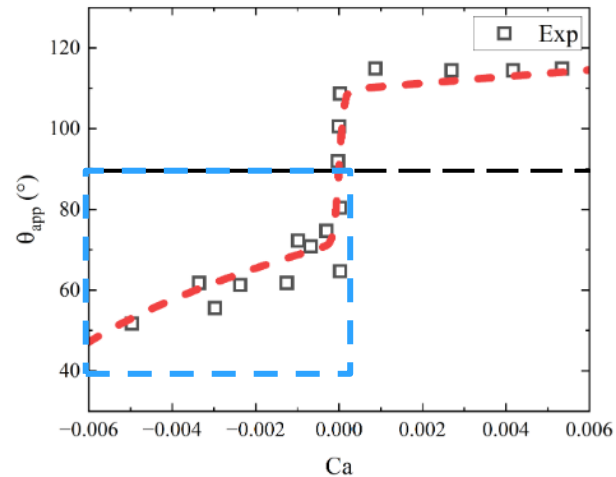
[2] Dwivedi et al. Physical Review Fluids, 2022, 7(3): 034002.

5. Bubble growth in oversaturated liquids

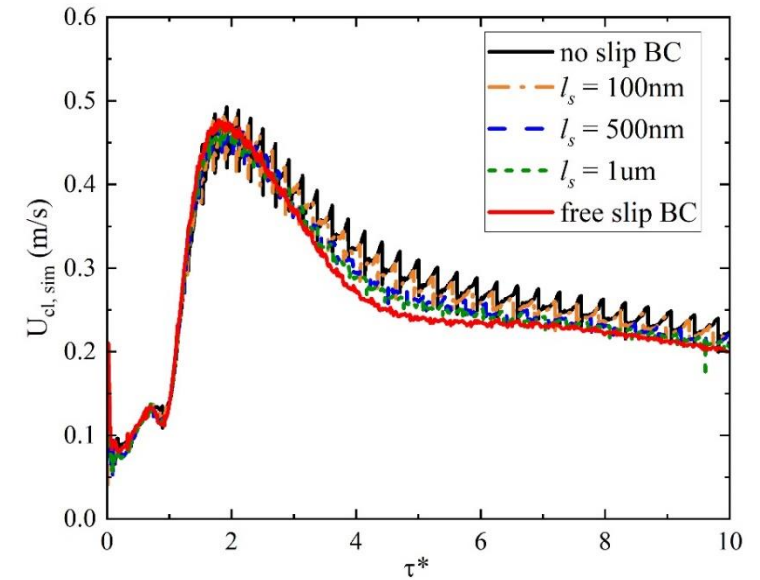
Validation

Initial setup:

- Oxygen bubble in oversaturated water;
- Bubble radius from 10 to 100 μm ;
- Initial contact angle: 90° ;
- Oversaturation ratio: $\zeta = \frac{c_b - c_s}{c_s} = 7$;
- Dynamic wetting curve:



Mesh size



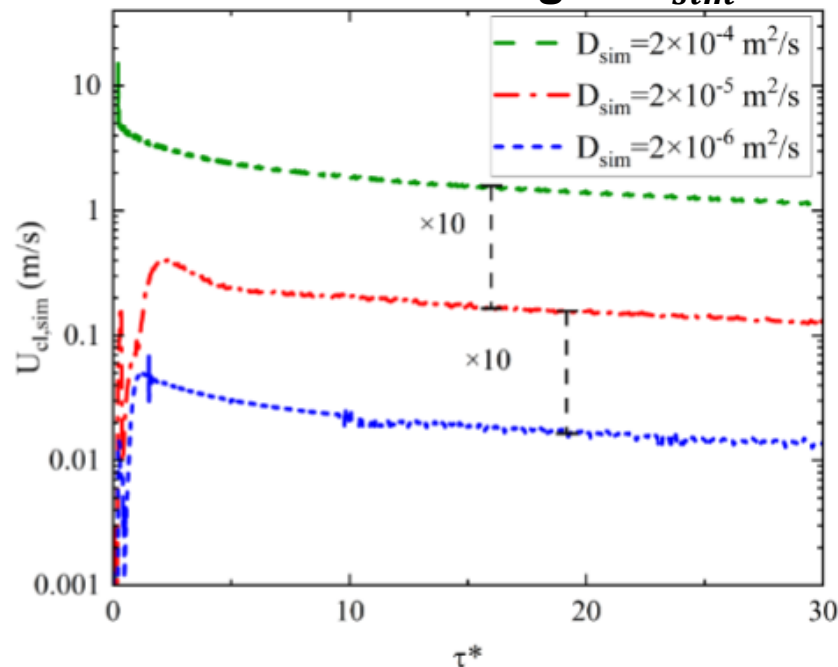
Navier slip BC

5. Bubble growth in oversaturated liquids

Issue of slow growth rates

	Boiling	Oversaturation Growth
Mass transfer rate	$10^{-3} \sim 10^{-1} \text{ kg/m}^2 \cdot \text{s}$	$10^{-7} \sim 10^{-3} \text{ kg/m}^2 \cdot \text{s}$
Timescale	Milliseconds to seconds	Seconds to Minutes
Dominant force	Inertia force	Surface tension force

Use an enlarged D_{sim}



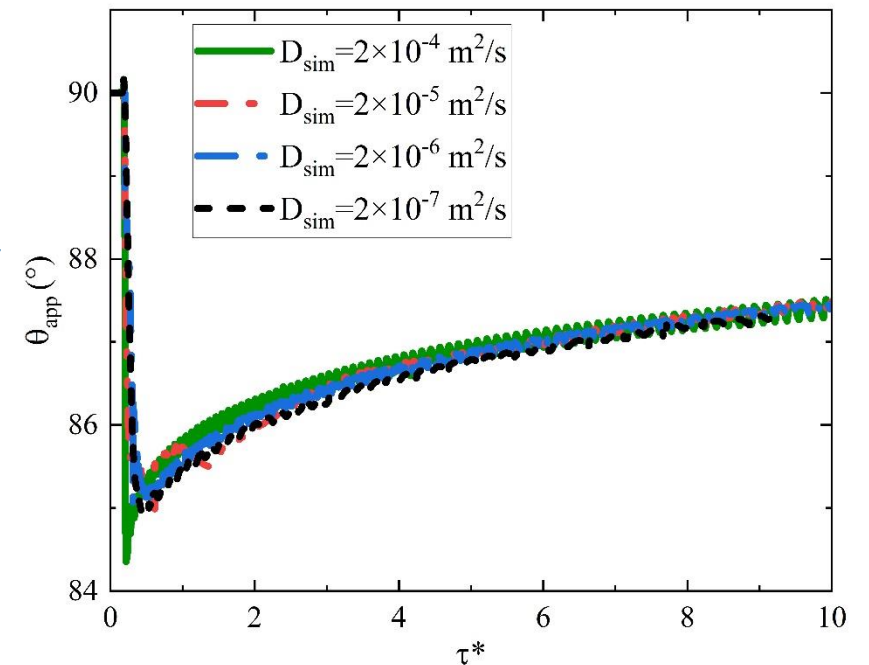
$$We = \frac{\rho_l U_{cl,sim}^2 R_0}{\gamma} < 1$$

Dynamic wetting →
Rescaling contact velocity



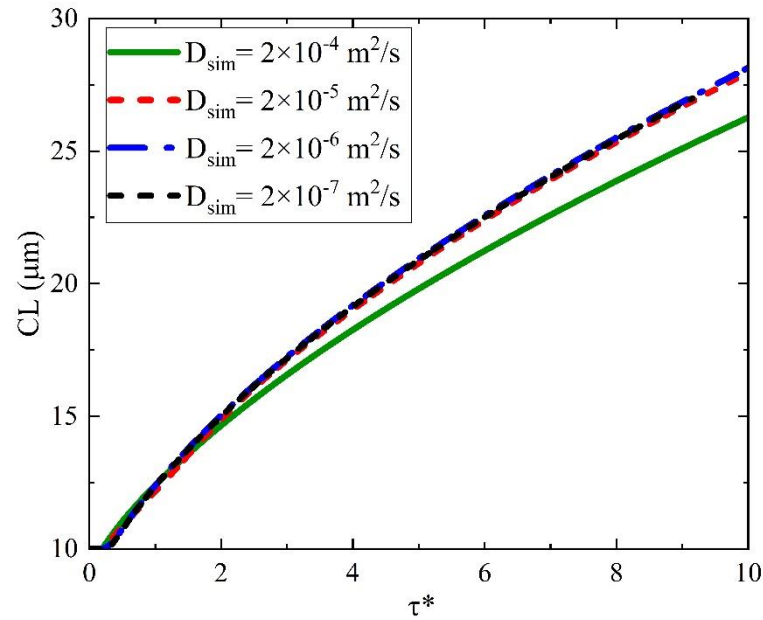
$$U_{cl,res} = U_{cl,sim} \cdot \frac{D}{D_{sim}}$$

$$t = t_{sim} \cdot \frac{D_{sim}}{D}$$

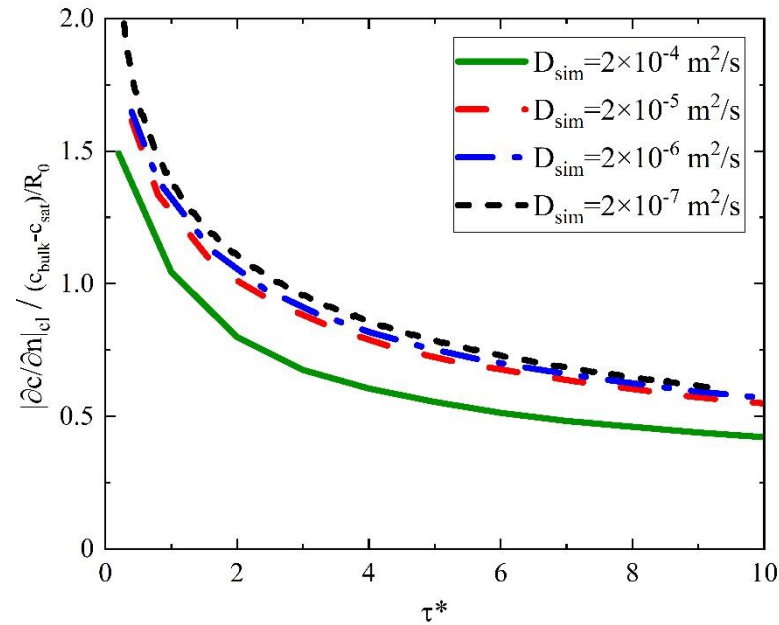


5. Bubble growth in oversaturated liquids

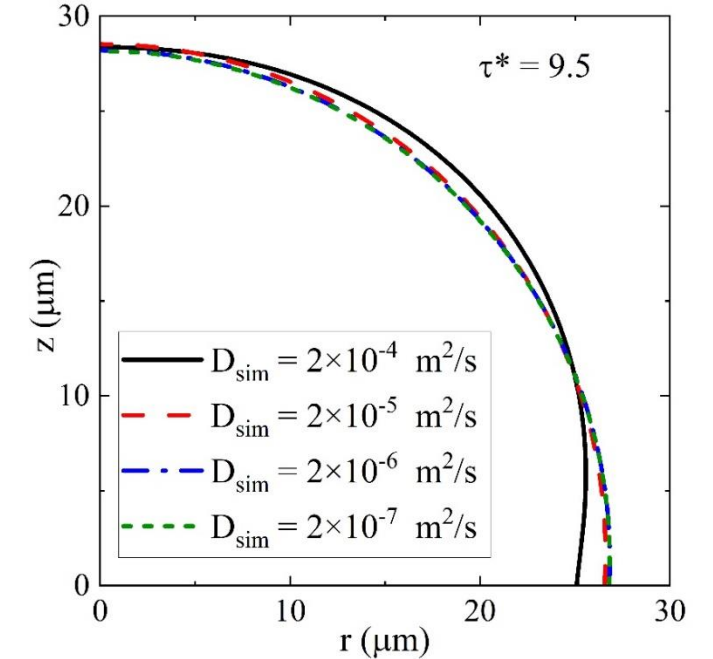
Issue of slow growth rates



Contact Line



Concentration gradient

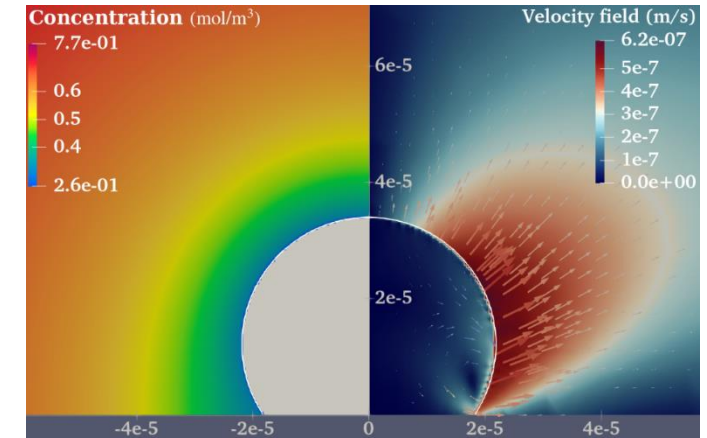
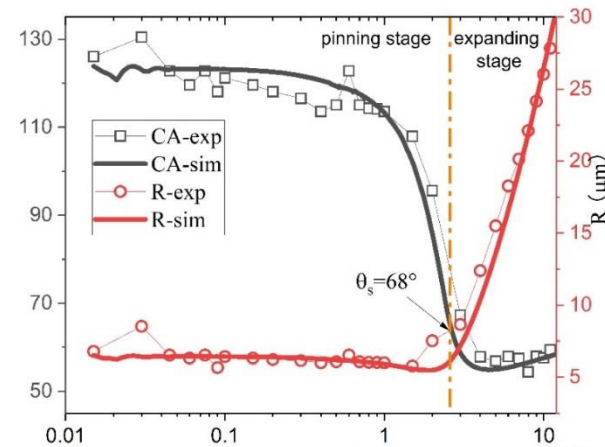
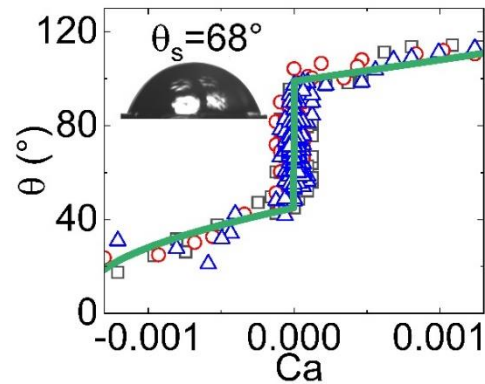


Bubble shapes

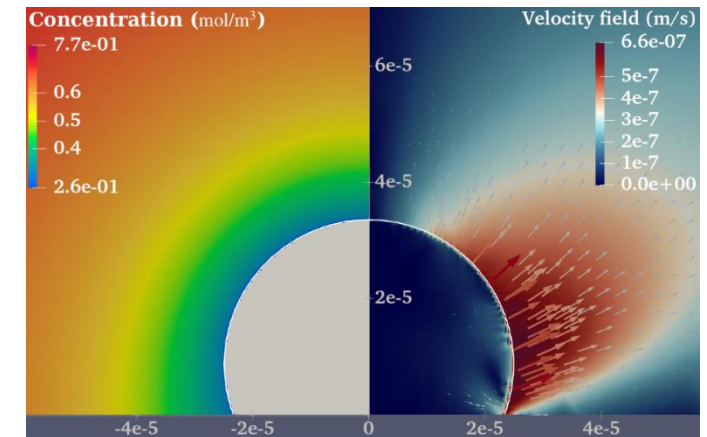
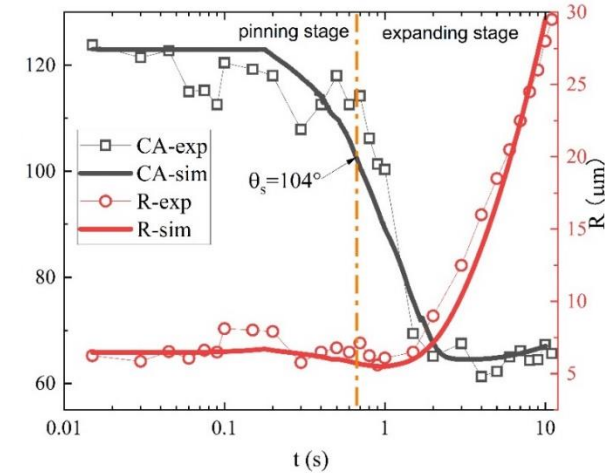
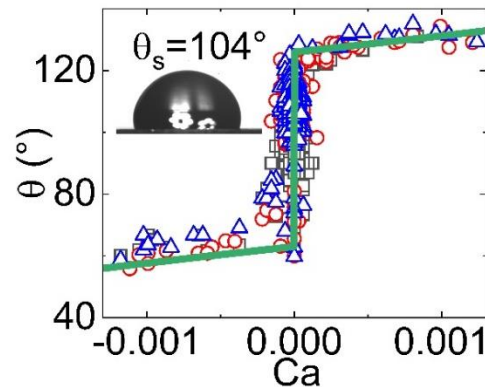
5. Bubble growth in oversaturated liquids

Validation with experimental results of single air bubble growth on two surfaces

Hydrophilic surface



Hydrophobic surface

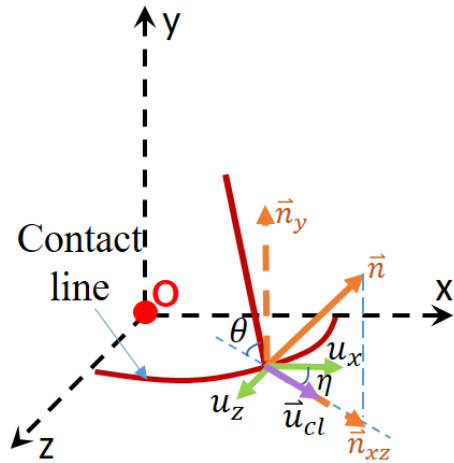


[1] Li et al. Colloids and Surfaces A: Physicochemical and Engineering Aspects 673 (2023): 131879.

[2] Han et al. Int. J. Multiph. Flow, 2025, accepted.

6. 3D Dynamic wetting

Methodology



Velocity projection

$$\eta = \tan^{-1} \left(\frac{n_z}{n_x} \right)$$

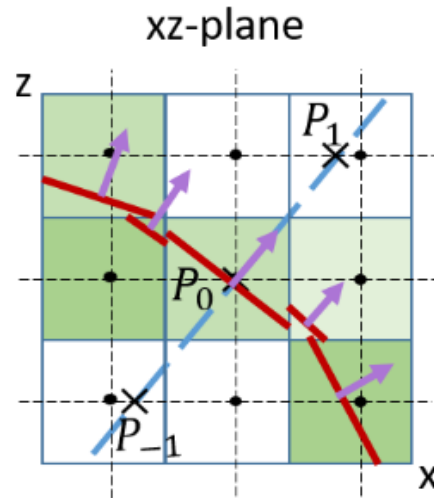
$$\vec{u}_{cl} = (u_x \cos \eta + u_z \sin \eta) \vec{e}_\eta$$

If $\vec{u}_{cl} \cdot \vec{n}_{xz} > 0$, advancing
If $\vec{u}_{cl} \cdot \vec{n}_{xz} < 0$, receding

$$\theta = \theta(\vec{u}_{cl})$$

Geometrical interface interpolation

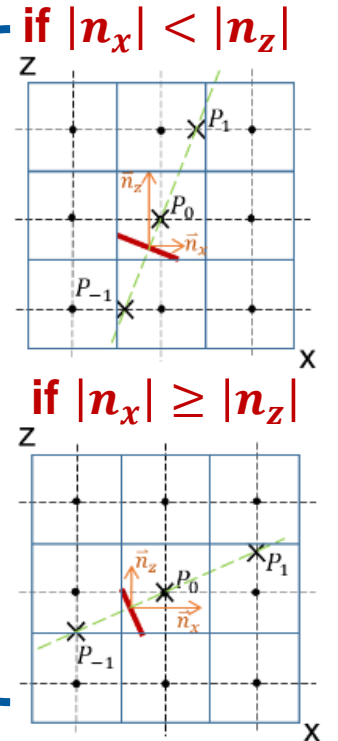
The contact angle need to be set at each point. $u_{cl,i} \rightarrow \theta_i$



Algorithm of contact line velocity interpolation

1. Identify all the interfacial cells at the first grid layer.
2. Compute the interface normal vector of \mathbf{n} each cell.
3. Compare the absolute values of n_x and n_z .
4. Compute the gradient of f in the normal direction.
$$\frac{\partial f}{\partial n} \approx \frac{f(P_1) - f(P_{-1})}{P_1 P_{-1}}$$
5. Perform a linear interpolation of x and z velocity components.

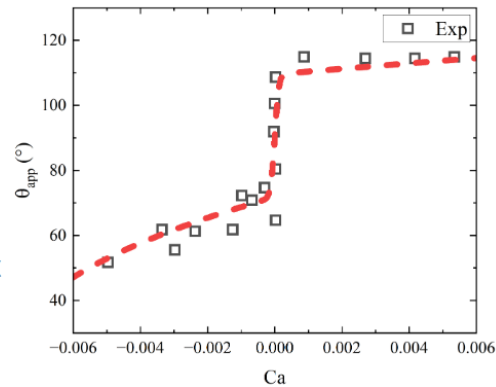
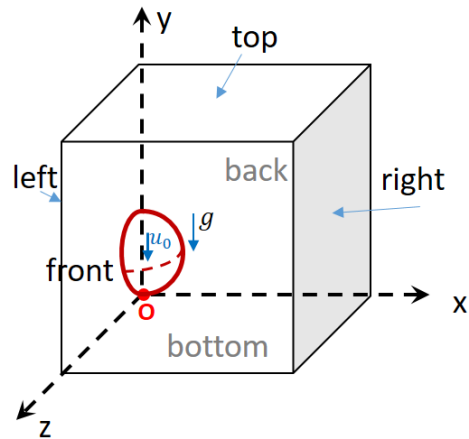
$$u_{x/z,interp} = u_{x/z}(P_0) + \frac{u_{x/z}(P_0) - u_{x/z}(P_{adj})}{f_{P_0} - f_{P_{adj}}} (f_{0.5} - f_{P_0})$$



[1] Han et al. 2025, in preparation.

6. 3D Dynamic wetting

Case 1: A spreading droplet on a solid surface (low Weber number)



Weber number $We=31.7$

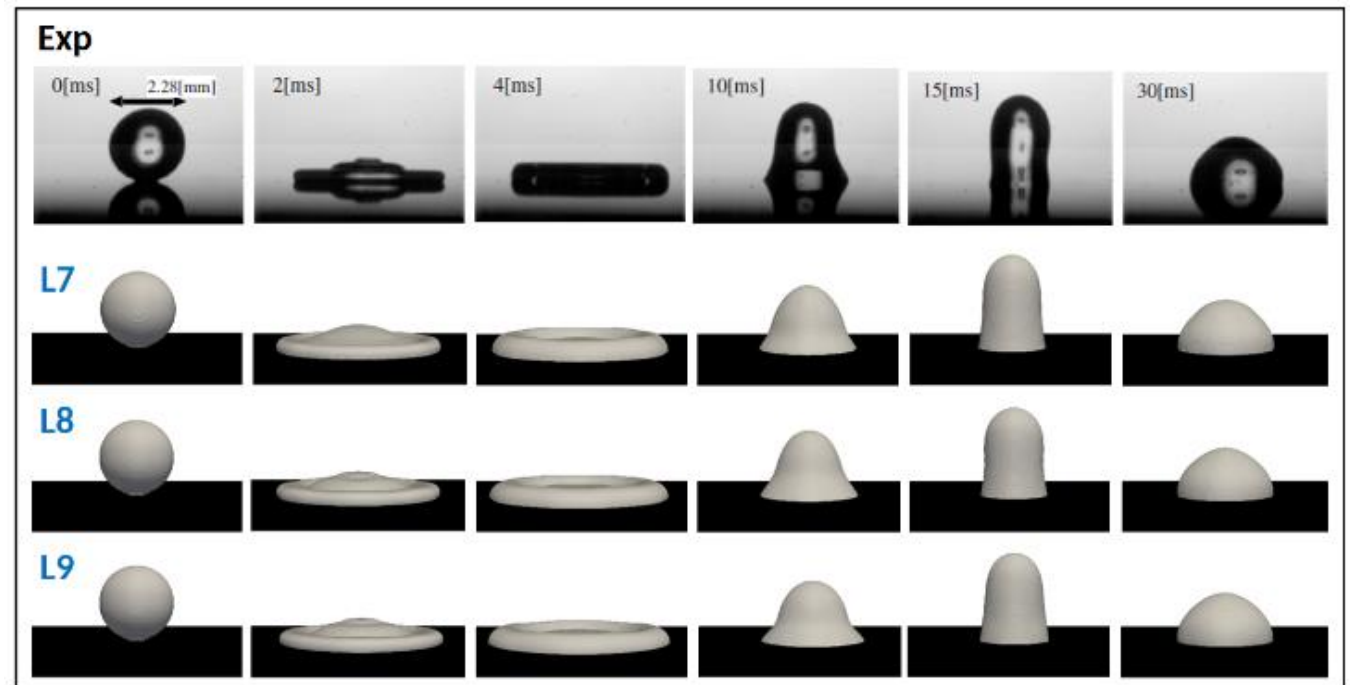
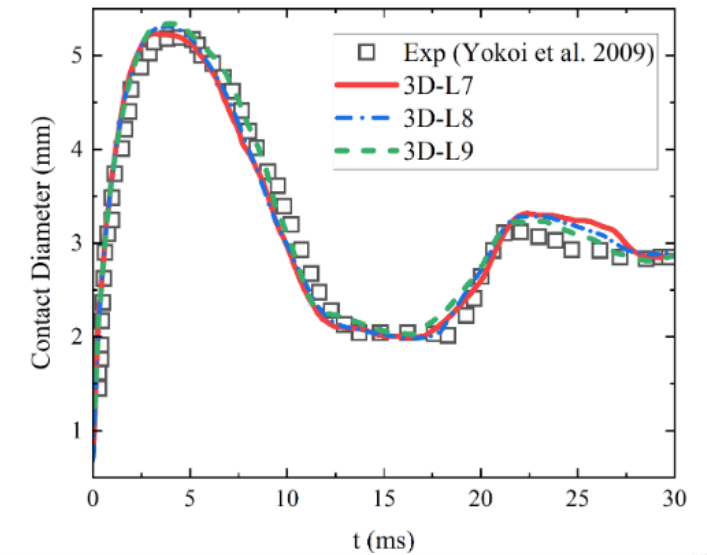
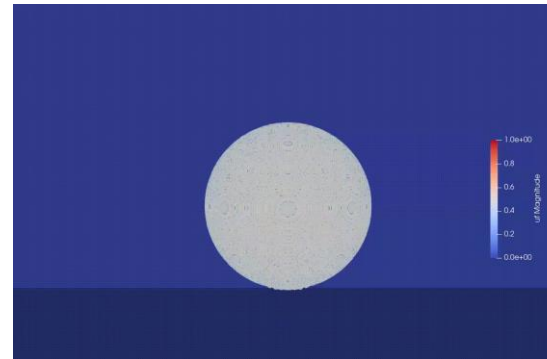
Initial radius: $R = 1.14 \text{ mm}$

Initial velocity: $V = 1.0 \text{ m/s}$

Bottom: no-slip BCs & dynamic wetting model

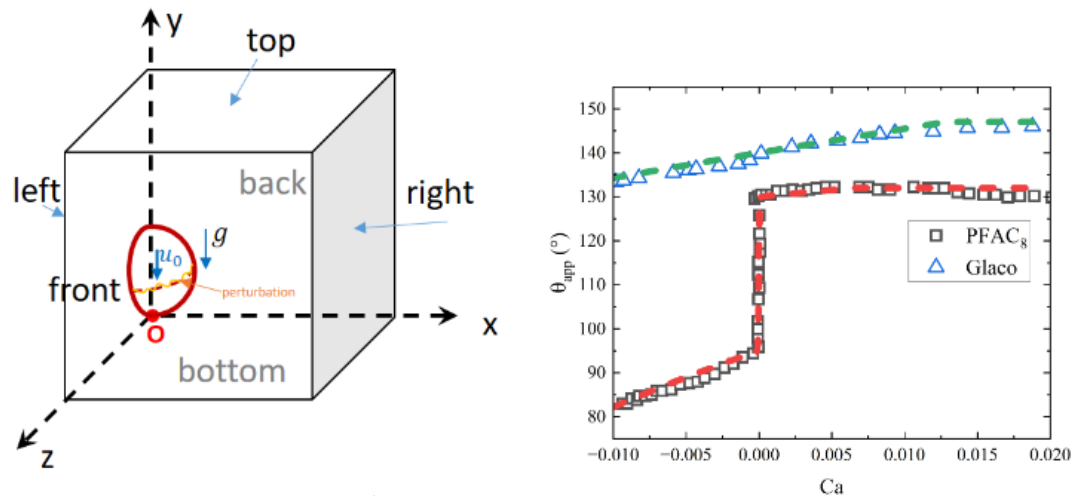
$\theta_s(^{\circ})$	$\theta_a(^{\circ})$	$\theta_r(^{\circ})$	$\xi_a(\text{Pa} \cdot \text{s})$	$\xi_r(\text{Pa} \cdot \text{s})$	C	ϵ
90	109.5	72	0.002	0.002	2×10^4	1.0×10^7

[1] Yokoi et al. Physics of Fluids, 2009, 21(7).



6. 3D Dynamic wetting

Case 2: A splashing droplet on hydrophilic surfaces (high Weber number)



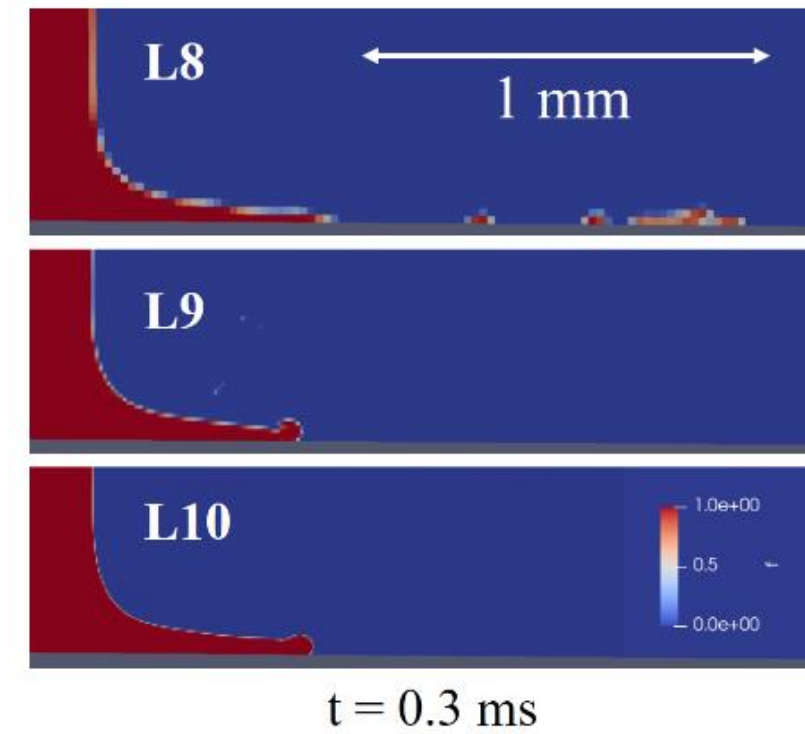
Initial perturbation of droplet radius

$$R_{0,p} = R_0 [1 + A_p \cos(2\pi Nx) \cos(2\pi Nz)]$$

Bottom: no-slip BCs & dynamic wetting model

	$\theta_s(^{\circ})$	$\theta_a(^{\circ})$	$\theta_r(^{\circ})$	$\xi_a(\text{Pa} \cdot \text{s})$	$\xi_r(\text{Pa} \cdot \text{s})$	C	ϵ
PFAC ₈	120	130	95	0.0001	0.01	2×10^4	1.0×10^4
Glaco	140	147	133	0.0025	0.0025	1	1.0×10^4

	R_0 (mm)	u_0 (m/s)	We
PFAC ₈	1.224	2.34	187
Glaco	1.356	2.09	167

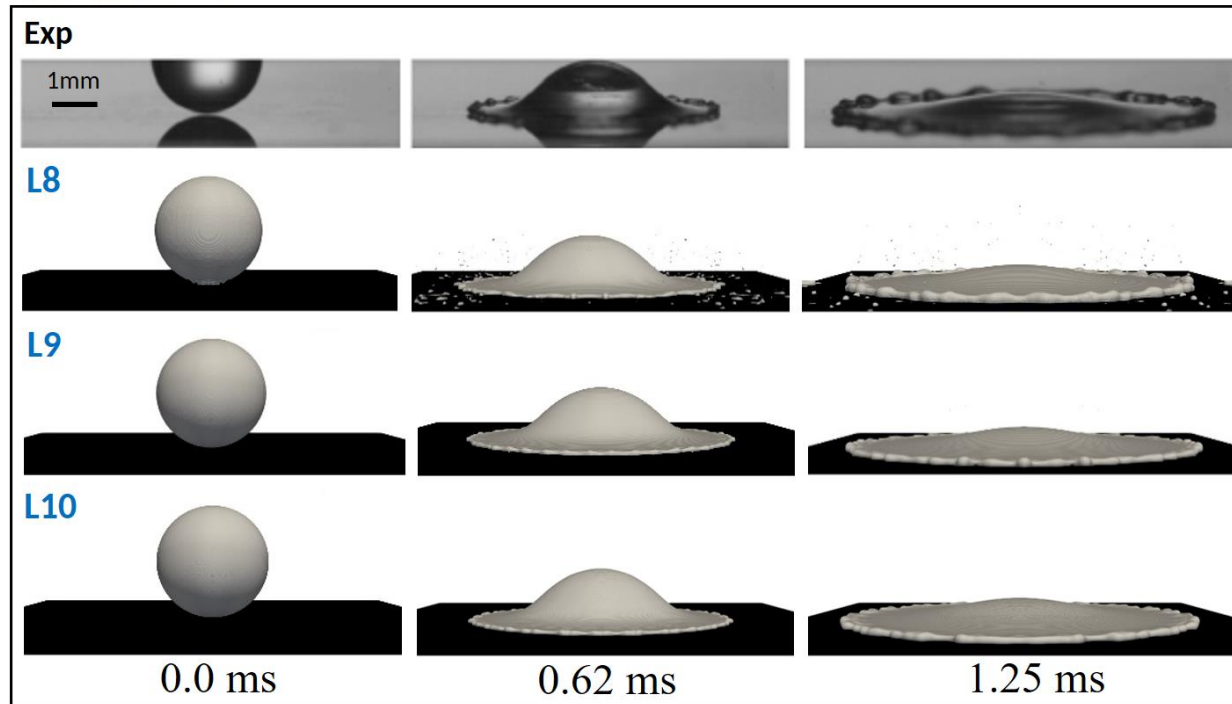


[1] Quetzeri-Santiago et al. Physical review letters, 2019, 122(22): 228001

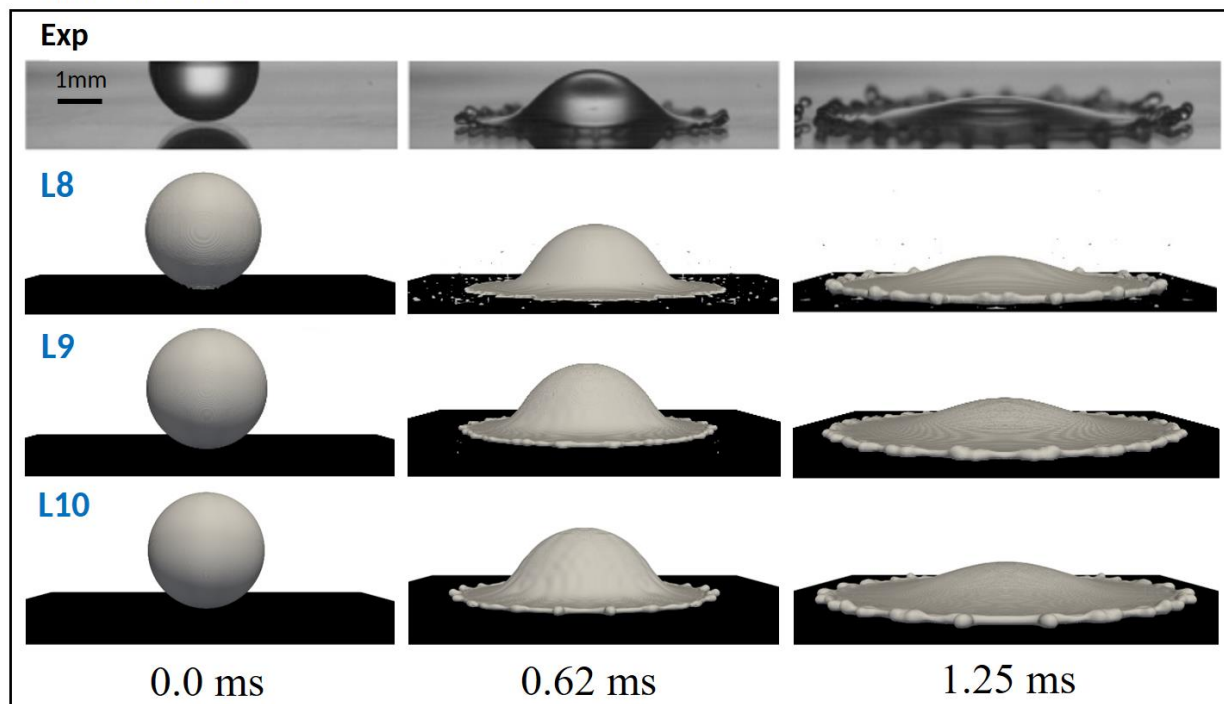
6. 3D Dynamic wetting

Case 2: A splashing droplet on hydrophilic surfaces (high Weber number)

Water on PFAC8



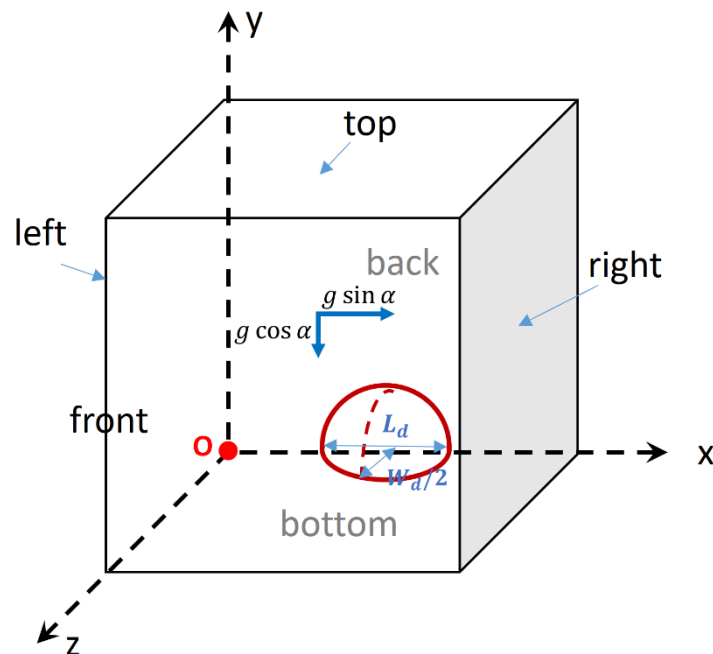
Water on Glaco



[1] Quetzeri-Santiago et al. Physical review letters, 2019, 122(22): 228001

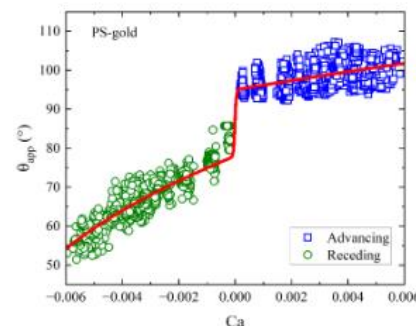
6. 3D Dynamic wetting

Case 3: A sliding droplet on inclined surfaces

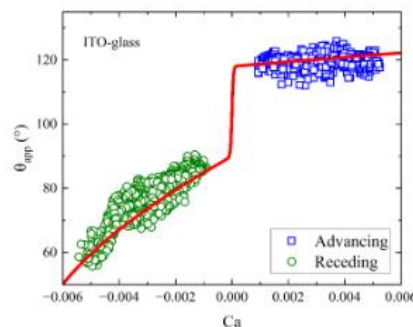


Initial radius 2.5 mm
Static contact angle
Inclined angle: $\alpha=25-70^\circ$

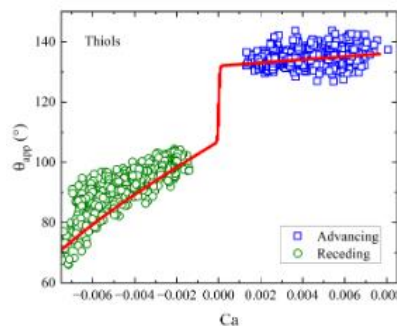
PS-gold



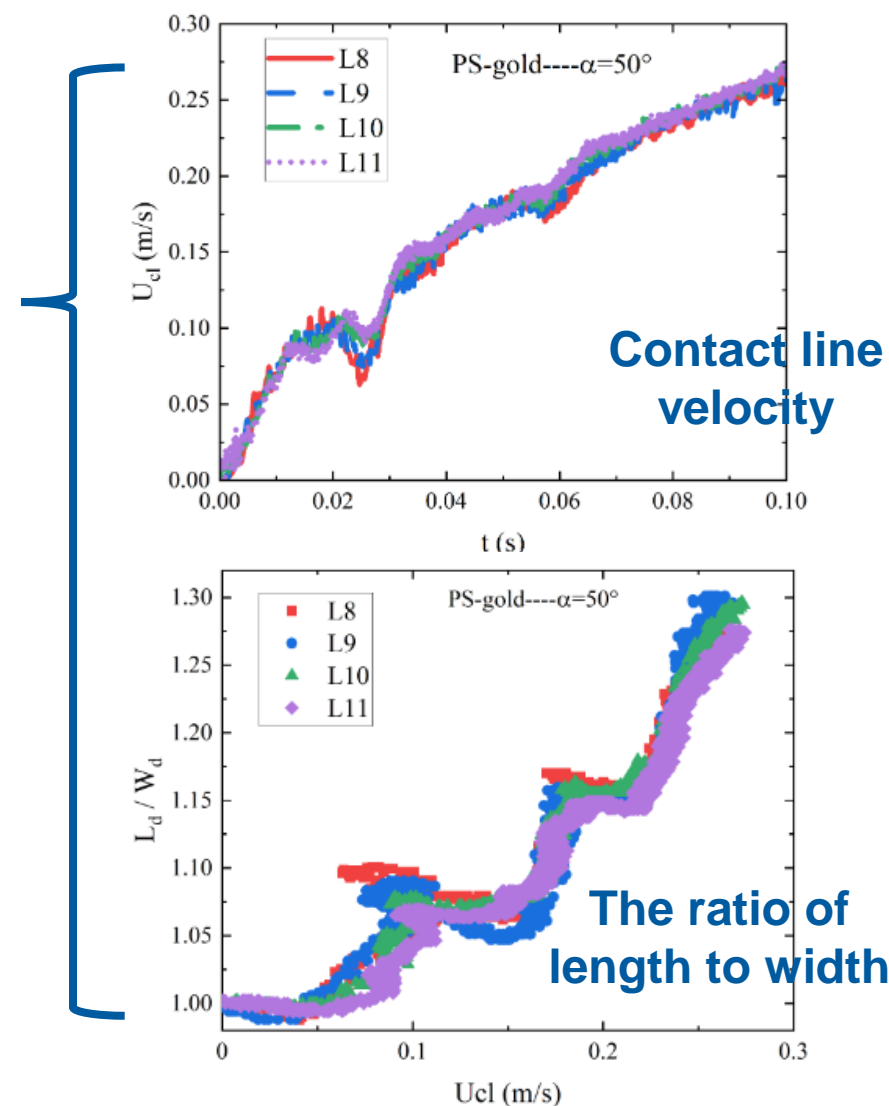
ITO-glass



Thiols



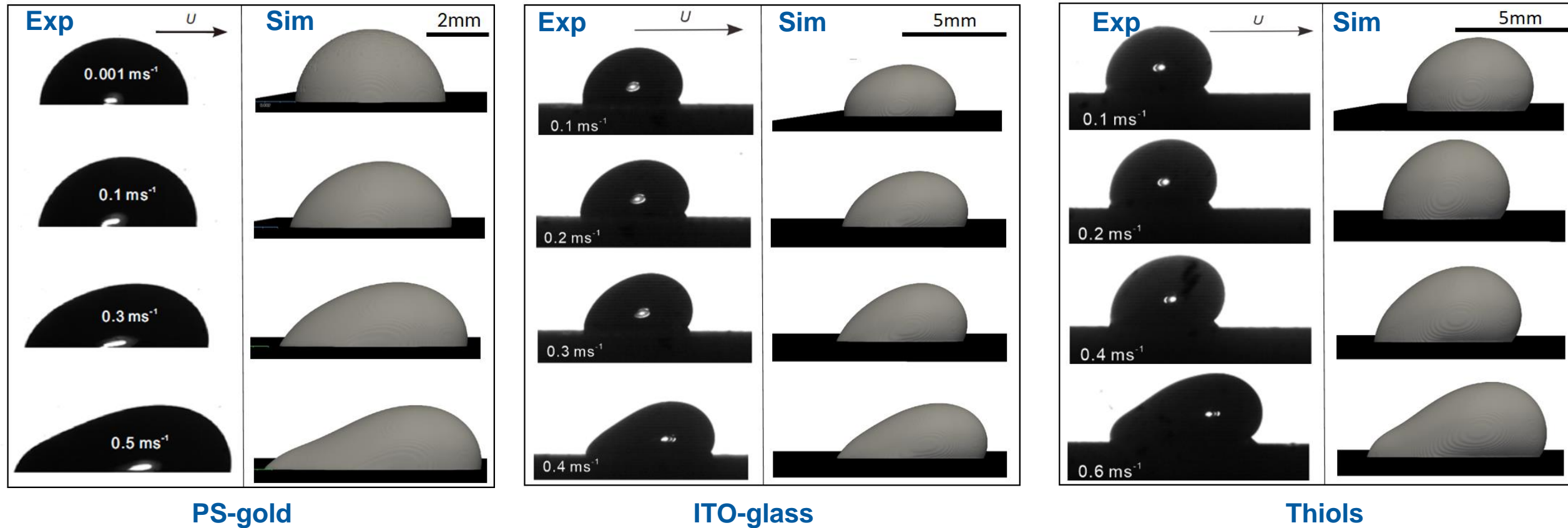
Resolution tests



[1] Li et al. Nature communications, 2023, 14(1): 4571.

6. 3D Dynamic wetting

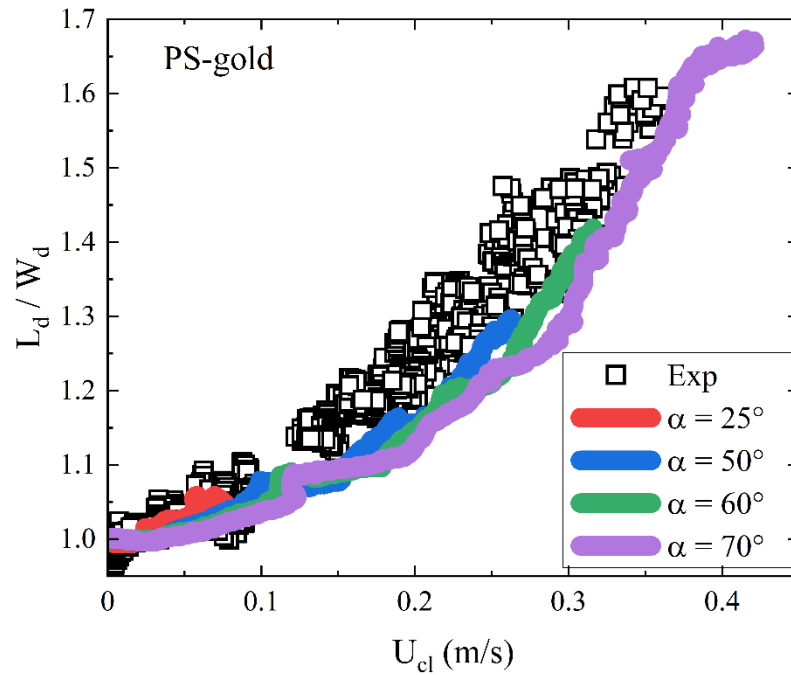
Case 3: A sliding droplet on inclined surfaces



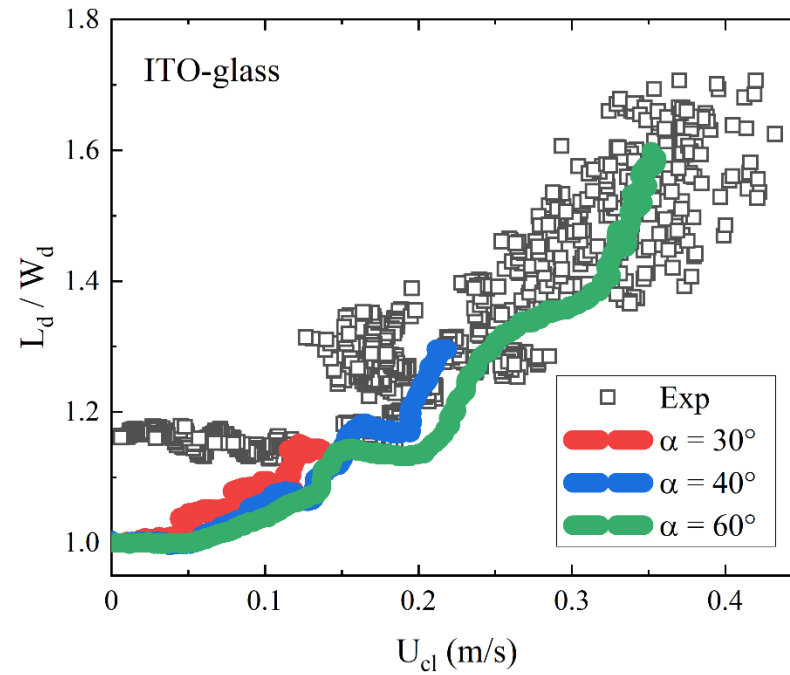
[1] Li et al. Nature communications, 2023, 14(1): 4571.

6. 3D Dynamic wetting

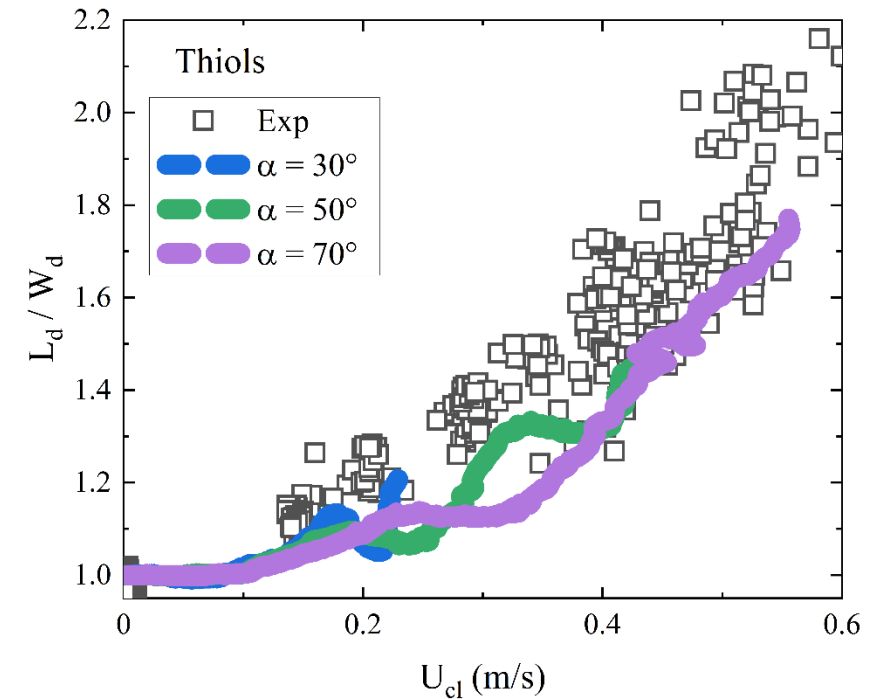
Case 3: A sliding droplet on inclined surfaces



PS-gold



ITO-glass



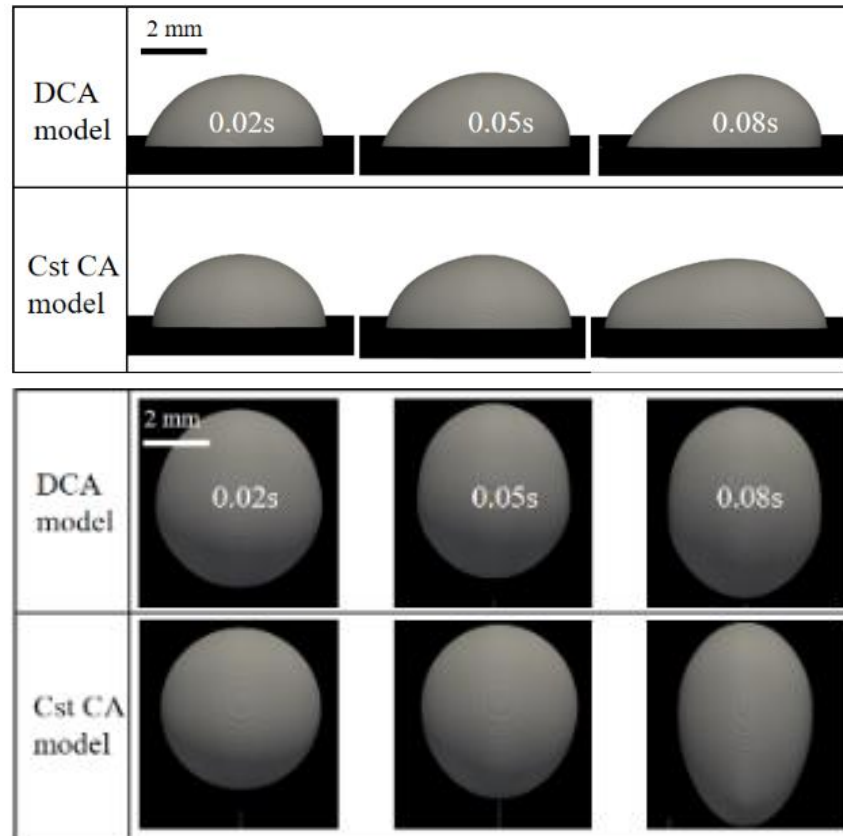
Thiols

[1] Li et al. Nature communications, 2023, 14(1): 4571.

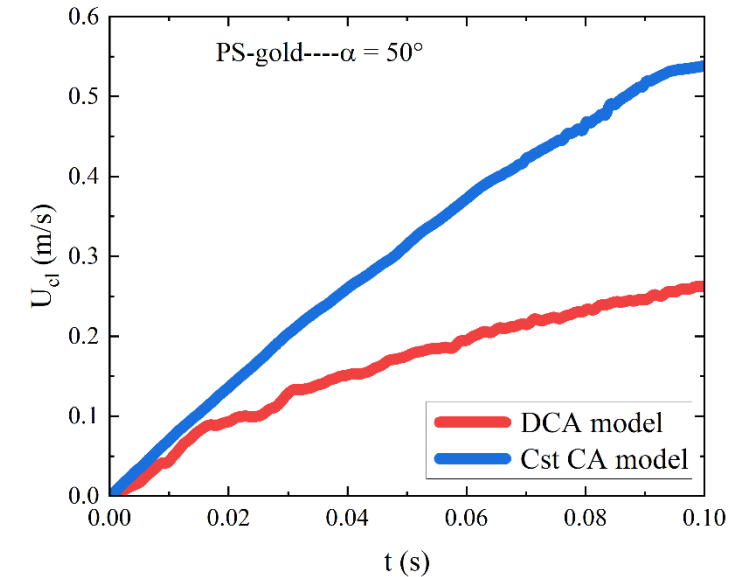
6. 3D Dynamic wetting

Case 3: A sliding water droplet on inclined surfaces

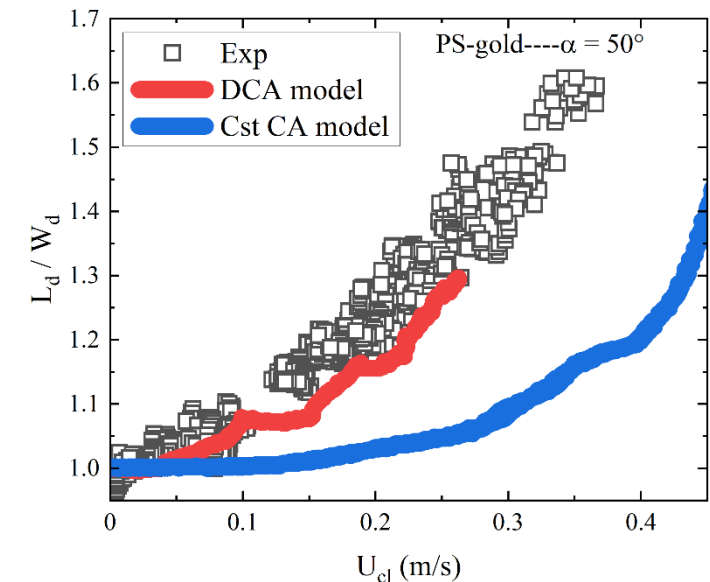
Dynamic vs Static models



Contact line velocity



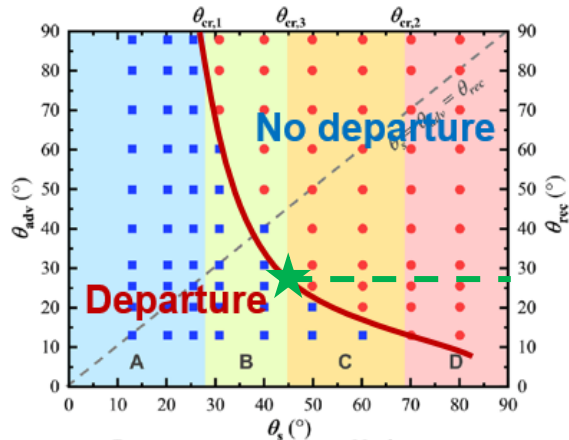
The ratio of length to width



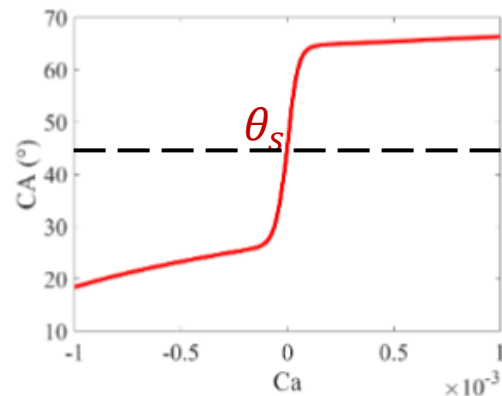
[1] Li et al. Nature communications, 2023, 14(1): 4571.

7. 3D Dynamic wetting

Bubble coalescence on a hydrophilic surface



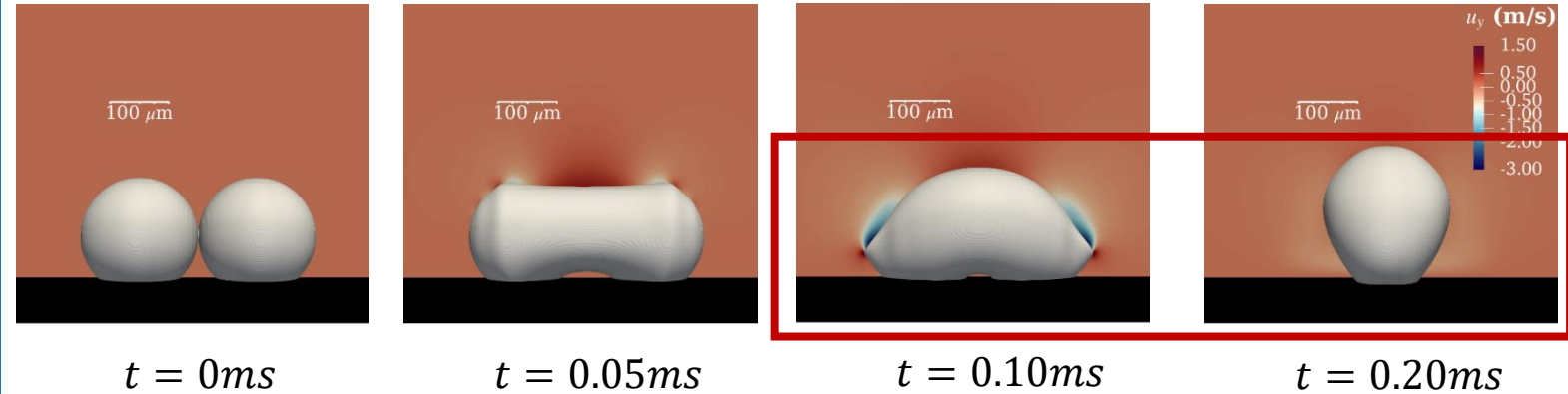
[1] Zhao et al. Langmuir 38.34 (2022): 10558-10567



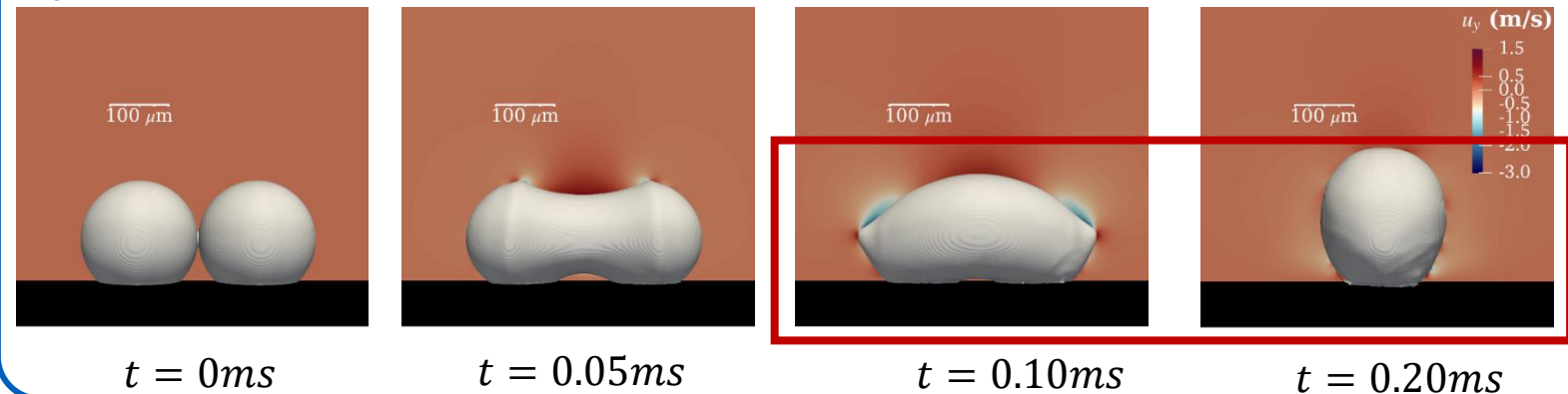
$\theta_s = 45^\circ$ CAH = 40°

Air-water: $R_0 = 100 \mu\text{m}$

Static model ($\theta_s = 45^\circ$)



Dynamic model ($\theta_s = 45^\circ$) CAH = 40°

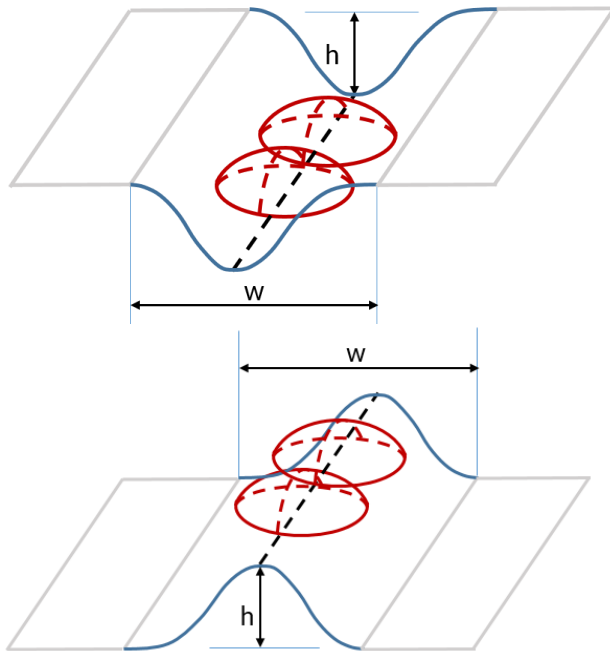


7. Bubble coalescence on structured surfaces

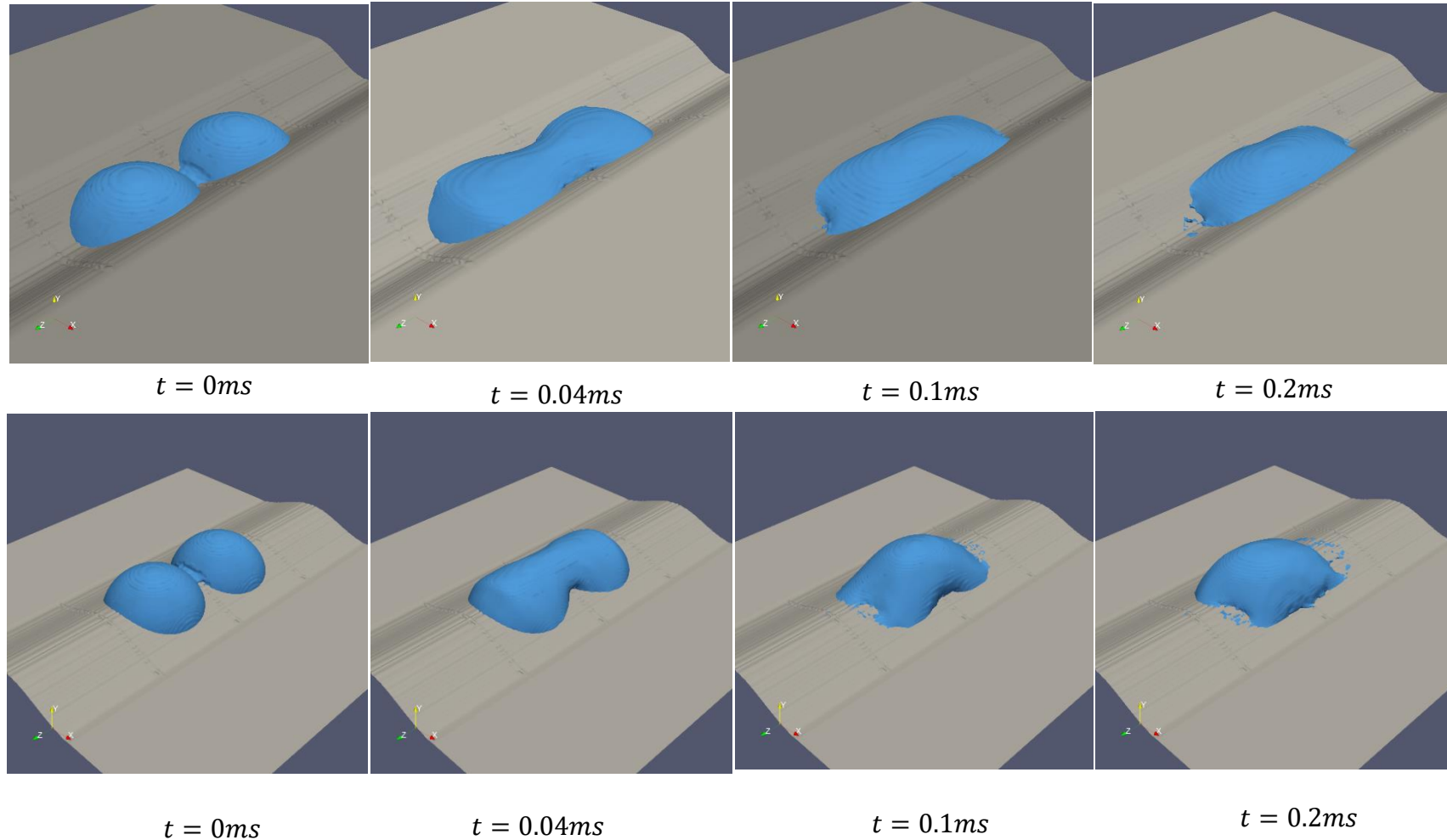
Static contact angle model

[1] Tavares et al. Computer & Fluids (2024)

(Embedded Boundary Method)



$h=40\mu\text{m}$, $w=200\mu\text{m}$
 $R_0 = 100\mu\text{m}$, $CA = 120^\circ$



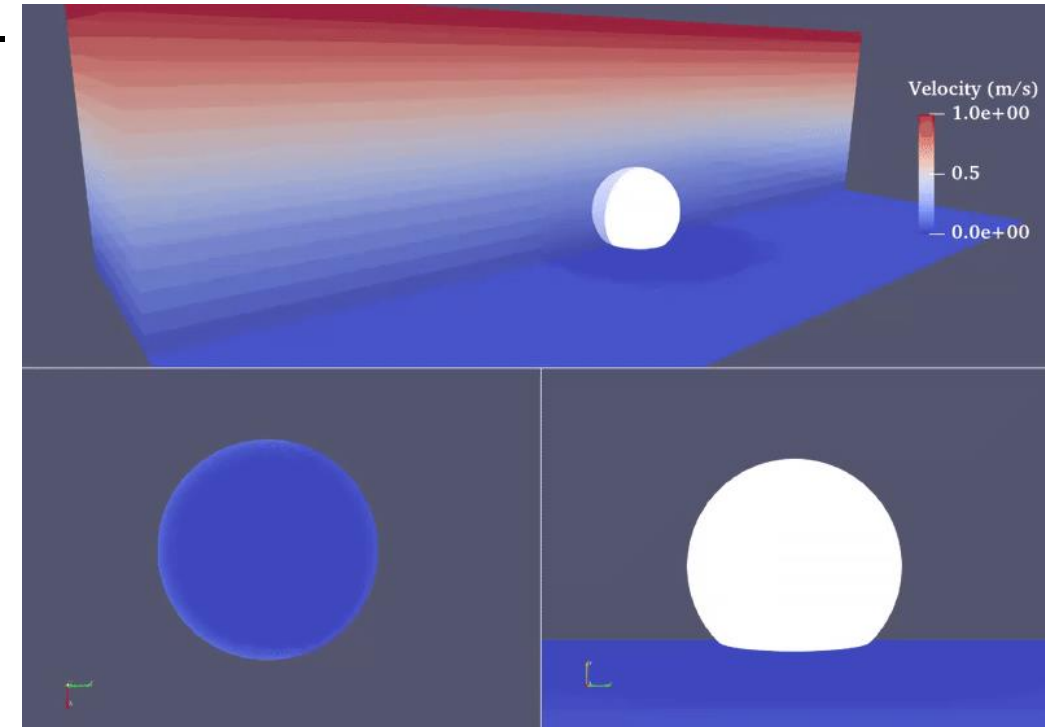
8. Conclusions and Outlook

Conclusions:

- A dynamic wetting model is implemented in 2D and 3D.
- Validated for oversaturation driven bubble growth.
- Validated for droplet spreading, splashing, and sliding.

Outlook:

- Bubble coalescence on different surfaces.
- Bubble detachment.
- Bubbles in shear flow.



Thanks for listening!

Email: yi.han@hzdr.de

Acknowledgment: The project H2Giga-SINEWAVE-Oxysep



AP1. Dimensionless equations

$$\text{Re} = \frac{\rho_l D}{\mu_l}, \quad \text{We} = \frac{\rho_l D^2}{\gamma R_0}, \quad \text{Fr} = \frac{D}{\sqrt{g R_0^3}}.$$

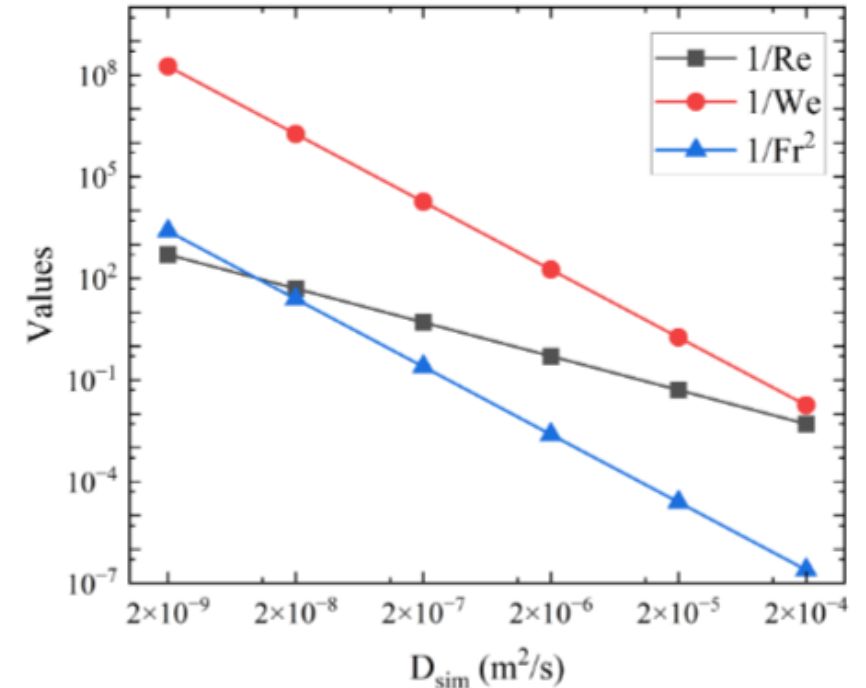


$$\nabla^* \cdot \vec{u}^* = \frac{\zeta}{\text{He}(1 - \rho_g^*/\rho^*)} (1 - \rho_g^*) \frac{\partial c^*}{\partial \vec{n}_\Sigma} \delta_\Sigma^*,$$

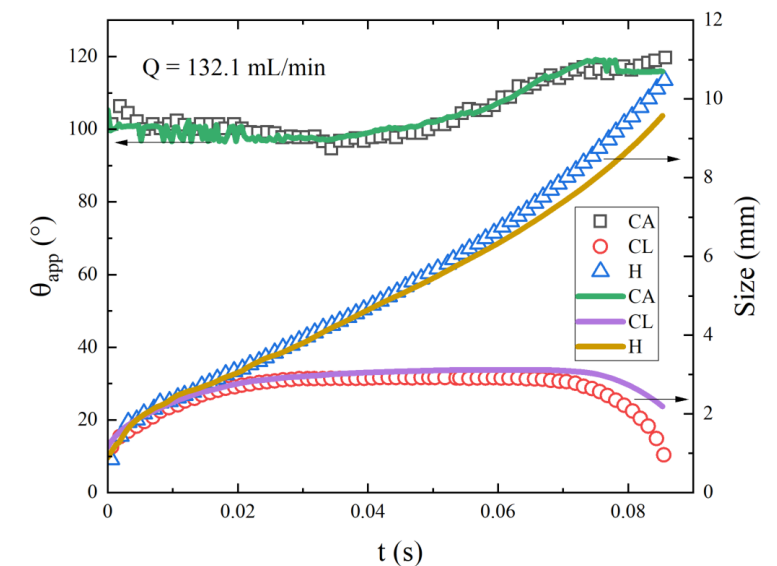
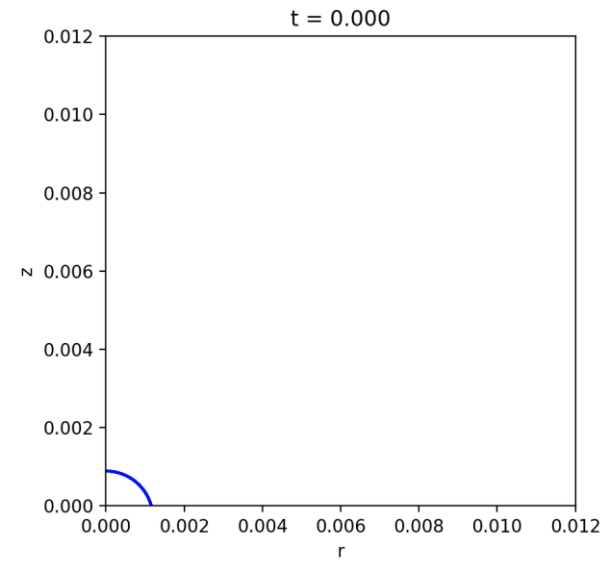
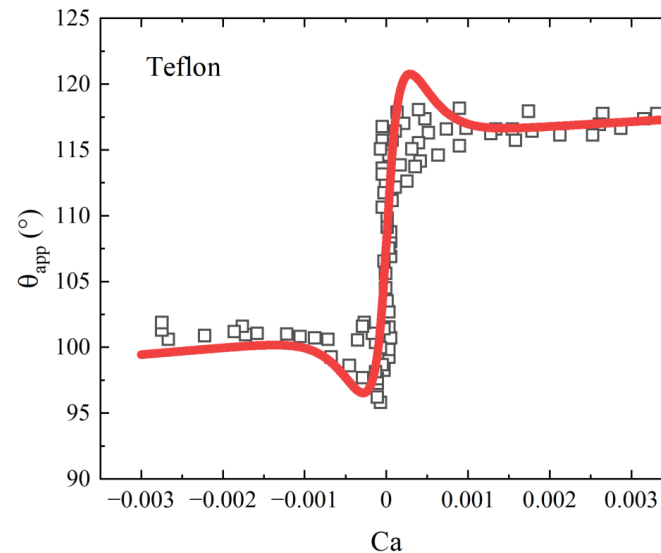
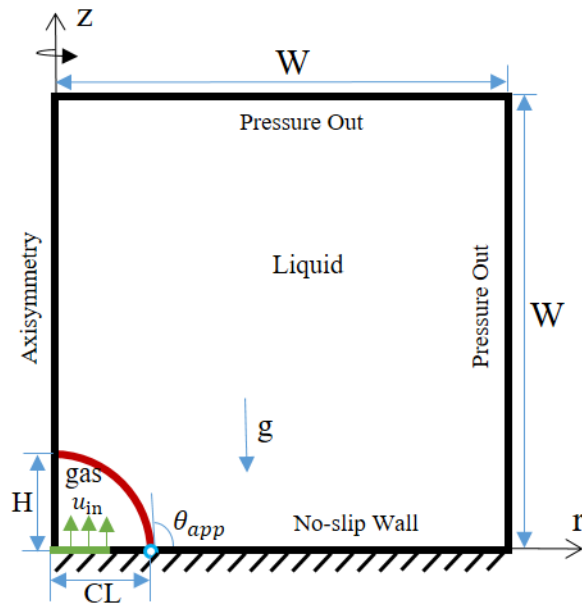
$$\frac{\partial \vec{u}^*}{\partial \tau^*} + \vec{u}^* \cdot \nabla^* \vec{u}^* = -\frac{\nabla^* p^*}{\rho^*} + \frac{1}{\rho^* \text{Re}} \nabla^* \cdot \{ \mu^* [\nabla^* \vec{u}^* + (\nabla^* \vec{u}^*)^T] \} + \frac{\kappa^* \vec{n}_\Sigma \delta_\Sigma^*}{\rho^* \text{We}} + \frac{\vec{z}'}{\text{Fr}^2 |\vec{z}|},$$

$$\frac{\partial \alpha}{\partial \tau^*} + \nabla^* \cdot (\alpha \vec{u}^*) = -\frac{\zeta}{\text{He}(1 - \rho_g^*/\rho^*)} \rho_g^* \frac{\partial c^*}{\partial \vec{n}_\Sigma} \delta_\Sigma^*,$$

$$\frac{\partial c^*}{\partial \tau^*} + \vec{u}^* \cdot \nabla^* c^* = \nabla^* \cdot (\nabla^* c^*) - \frac{1}{(1 - \rho_g^*/\rho^*)} \frac{\partial c^*}{\partial \vec{n}_\Sigma} \delta_\Sigma^*,$$



AP2. Bubble departure on solid surface



Experiments in Fluids (2020) 61:83
<https://doi.org/10.1007/s00348-020-2919-7>

RESEARCH ARTICLE

Influence of wetting conditions on bubble formation from a submerged orifice

H. Mirsandi¹ · W. J. Smit¹ · G. Kong¹ · M. W. Baltussen¹ · E. A. J. F. Peters¹ · J. A. M. Kuipers¹

Received: 16 October 2019 / Revised: 13 January 2020 / Accepted: 13 February 2020 / Published online: 2 March 2020
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Dimensional parameters

$\rho_{l} = 998$
 $\rho_{g} = 1.25$
 $\mu_{l} = 1.0e-3$
 $\mu_{g} = 1.82e-5$
 $F_{\sigma} = 0.0725$
 Domain width (W): 12 mm
 Gravity: 9.8 m/s²
 $R_{injec} = 0.5$ mm